## Finding Critical Scenarios for Automated Driving Systems: The Data Extraction Form

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This is the data extraction form for the systematic mapping study to find critical scenarios for automated driving systems. Table 1 lists all the acronyms used in the main paper. The extracted data from the primary studies is structured in the rest of the tables according to the taxonomy defined in Section 4 of the main paper. Table 2 shows how the content in these tables links to the taxonomy. Primary studies in Tables 2 to 6 correspond to the five clusters defined in Section 6 of the main paper.

Please note that some primary studies in these tables are classified as out of the scope of the literature study. These studies are marked in the Purpose column. Primary studies in Tables 7 and 8 are eventually considered as out of the scope. The tables are designed aligned with the taxonomy proposed in Section 4 of the main paper.

Table 1. List of	f acronyms	s used in the	systematic	mannina	study

SOI	System Of Interest	KPI	Key Performance Indicator	DSE	Design Space Exploration
AEB	Automatic Emergency Braking	NCAP	European New Car Assessment Programme	SBT	Search-based Testing
LKA	Lane Keep Assist	FMEA	Failure Modes and Effects Analysis	NDS	Naturalistic Driving Study
ACC	Adaptive Cruise Control	V2X	Vehicle to Everything Communication	FOT	Field Operational Test
TTC	Time To Collision	RQ	Research Question	VAAFO	Virtual Assessment of Automation in Field Operation
HARA	Hazard Analysis and Risk Assessment	V&V	Verification and Validation	QOS	Quality Of Service
RRT	Rapidly Exploring Random Trees	FTA	Fault Tree Analysis	ODD	Operational Design Domain
MDP	Markov Decision Process	CV	Computer Vision	CSI	Critical scenario Identification
RSS	Responsibility Sensitive Safety	ADS	Automated Driving System	GTA	Grand Theft Auto
GPS	Global Positioning System	ADAS	Advanced Driving-Assistance System		
NLP	Natural Language Processing	FuSa	Functional Safety		
RNN	Recurrent Neural Networks	SOTIF	Safety of the Intended Functionality		

Table 2. Links between the taxonomy in the main paper and the content in the data extraction form

	Elements in the taxonomy in the main paper	Elements in the data extraction form		
	System of Interest	Purpose -> SOI		
_ <u> </u>	Phase	Purpose -> Phase		
litic	Purpose	Purpose		
rob	Targeted ODD	Purpose -> ODD		
م م	Definition of Criticality	Criticality definition & Surrogate Measure		
	Level of Abstraction	Solution -> Input Sce. AND Solution -> Output Sce.		
	Scenario Space Construction	Scenario definition		
o	Purpose Purpose Purpose Purpose Purpose -> ODD  Definition of Criticality Criticality definition  Level of Abstraction Solution -> Input Scenario Space Construction -> Content Scenario Space Construction -> Representation Solution -> Input Scenario Space Exploration Solution Soluti	Scenario definition -> Covered layers		
Ē	Scenario Space Construction -> Representation	Solution -> Input Sce. AND Solution -> Output Sce. AND Scenario definition		
Sol	Scenario Space Exploration	Solution		
	Required Information	Validation & other key observations -> Required knowledge		
Evaluati	on	Validation & other key observations -> Validation		

Table 3. Exploring logical scenarios without parameter trajectories

#	Purpose	Scenario definition	Criticality definition & Surrogate Measure	Solution	Validation & other key observations
[1][	Activity: formalization (Ontology	A scenario is defined as the development of	The criticality of scenarios is evaluated	Input Sce.: A logical scenario described with	Required knowledge:
2][3	meta-model) & Instantiation &	the initial scene over time.	based on the different KPIs (e.g. TTC, yaw	the UML-based ontology model	1. A given functional scenario from
]	criticality check		rate, longitudinal and lateral	Output Sce.: critical concrete scenarios	EuroNcap
	Phase: system verification /	The author utilizes a domain ontology to	acceleration and deceleration) of the		2. Ontology of the environment
	component verification, depending	capture the environment of the system	ADAS/AD functions.	Method: makes use of ontologies for	description for the formalization
	on the type of simulation (e.g., MIL,	under test (SUT) in a degree of detail. The		describing the environment of autonomous	3. Functional models of the AD
	SIL or HIL)	ontology consists of static (e.g. road type,		vehicles and convert them to input models	system
	SOI: decision-making and control	infrastructure, lanes, road marking, traffic		for combinatorial testing. The input model	4. Predefined KPIs
	system	rules) and dynamic information (e.g.		includes all the parameters and their	5. A Simulator (VTD)
		objects type, speed, acceleration, direction)		representative values including their	
	A general framework to	of the environment. The ontology for the		relations and constraints. The combinatorial	Validation:
	automatically test the whole AD	system under test is constructed using UML		test suite comprises abstract test cases that	A case study to show that this
	function(s) as a black box, aiming at	as modeling language.		are mapped to concrete test cases that can	method can find critical and crashing
	finding critical scenarios, and			be executed using CO-simulation platform.	scenarios.
	thereby improve the AD	This paper proposes a UML-based Ontology		Criticality will be evaluated based on the	
	function(s).	meta-model, using which, one can propose		defined KPIs.	Similar paper:

		their own ontology according to their own case.  Covered layers: it depends on the final ontology. The given demo use case only considers layer 4 (including the initial states of the ego vehicle)		This paper considers <b>N-wise coverage</b> .	[4] Ponn2019a uses N-wise testing to generate test cases for the Lane Keeping Assist function (ADAS). It provides a detailed ontology of the logical scenario for this use case.
[5]	Activity: Instantiation & criticality check (requirement falsification) or refinement of a concrete scenario Phase: system verification SOI: the whole system  This paper presents a simulation-based testing framework for test case generation and falsification for the whole AD system or a particular function.	A scenario in this paper refers to one simulation run with fixed time interval. It includes the intended behavior of the ego vehicle.  A concrete scenario is a vector of relevant parameters such as the positions of other vehicles, the colors and models of other vehicles, etc.  Covered layers: 1 (fixed for each logical scenario), 4 (including the initial states of the ego vehicle), 5	In this paper, a critical scenario (in this paper it is call a glancing scenario) is defined as a boundary scenario between acceptable scenarios and unacceptable scenarios, e.g., a collision occurs with a small velocity.  The acceptance criteria are described in signal temporal logic (STL).  A concrete scenario will be run in a simulator to generate a simulation trace (a state trajectory). The simulation traces will be evaluated against a STL specification. The evaluation returns a value denoting the robustness of the satisfaction. If the value is positive and close to zero, it means that the scenario satisfies the specification, but it is very close to unsatisfaction. To this end, glancing scenarios are the ones whose robustness values are close to zero.  Identified critical (glancing) scenarios can be used as test cases for falsification.	Input Sce.: A logical scenario Output Sce.: critical concrete scenarios  Refinement: Input Sce.: A concrete scenario Output Sce.: a more critical concrete scenario by tuning the continues parameters.  The falsification process has two steps. The first step is to find all the glancing scenarios. The second step is to find collision scenarios around the glancing scenarios.  Combinatorial test generation is used for the first step to generate a covering array guaranteeing N-wise coverage. To do this, continues variables are uniformly discretized. Among all the scenarios in the covering array, glancing scenarios are selected.  The second step uses each identified glancing scenario as an initial point to optimize the continues variables to find more glancing scenarios.  The second step can also be considered as a refinement of a given concrete scenario.  This paper considers N-wise coverage.	Required knowledge:  1. A given logical scenario  2. Functional models of the ADS (as a black box)  3. A simulator (Webots)  4. Predefined specifications in STL  5. S-TaLiRo, a falsification tool to calculate the robustness value.  Validation:  A case study to show that the approach can generate glancing scenarios.  It assumes that glancing scenarios are more common than seriously hazardous scenarios.  It assumes that the glancing scenarios are avoidable by improving the functionality, and are hence more important.

					<u> </u>
[6]	Activity: Instantiation & criticality	Same as [5].	Not like [5], this paper tries to find	The searching method is the same as the one	Required knowledge:
	check (requirement falsification) or		scenarios with the lowest robustness value.	proposed in [5].	1. A given logical scenario
	refinement of a concrete scenario	Covered layers:1,4,5			2. Functional models of the ADS (as
	Phase: system verification		The requirements used for its case studies	This paper considers <b>N-wise coverage</b> .	black boxes)
	<b>SOI:</b> the whole system, decision-	Layer 1: Road	are:		3. A simulator (Webots)
	making and control system,	Layer 4: Ego vehicle, agent vehicle,	1. Not collide with an object (system-level)		4. Predefined requirements (defined
	perception system	pedestrian	2. Detect visible obstacle within a certain		by STL)
			time unit (sensor-level)		5. Sensor models, including CCD
	This paper extends [5].	Layer 5: e.g., building colors	3. Localization errors should provide		camera, lidar, and radar
			sufficient accuracy (defined by an error		6. Stochastic search optimization
	It introduces methods to use their		threshold) (sensor-level)		method for finding falsification
	framework to falsify the perception		4. A sensor-related fault should not lead to		
	systems (referring to their		a system-level fault (collision) (sensor-to-		Validation:
	requirement 2 and 3) and the		system level)		Compared to [5], 3 case studies are
	sensor fusion system (referring to		5. The vehicle should not do excessive		introduced in the paper to evaluate
	their requirement 4).		braking unnecessarily or too often		the performance of the method and
			(system-level performance)		describe how to use the results to
					enhance the development process.
			Different requirements can be used for		
			different use cases.		
[7]	Activity: Instantiation	A test scenario in this paper is specified by	In this paper, a scenario is critical if a small	Input sce.: A given logical scenario	Required knowledge:
	Phase: system verification	one scenario configuration, which covers the	change of its configuration leads to	Output sce.: critical concrete scenarios	A given logical scenario
	<b>SOI:</b> decision-making and control	environment, mission and vehicle	significant changes of the SUT		2. Functional models of the ADS
	system	parameters. It does not include the	performance.	Adaptive sampling, a learning- based testing	(as a black box)
		implementation of the SUT.		method, is used with simulation to generate	3. A simulator (APL Autonomy
	The proposed method is to		Changes of scenario configurations are	boundary pairs, which contains two similar	Toolkit)
	generate test cases for the	A scenario configuration is formally modeled	quantified by the distances in the	scenarios where the SUT will behave in two	,
	decision-making module of	as a vector in a state space of continuous and	configuration state space.	different performance modes.	Validation:
	autonomous systems, i.e., the SUT.	discrete values. This state space consists of			No validation. It only verifies the
		all the possible scenario configurations that	SUT performance is evaluated in a score	A surrogate model is used to improve the	performance of the proposed
	The generated test cases are	could be tested.	space, where each dimension is a	coverage of the sampling. It takes a set of	method.
	diverse and close to decision		performance metric, e.g., TTC, number of	samples as input and returns the estimated	
	boundaries, where minor changes	The distance between two scenario	way points reached, fuel consumption, etc.	diversity (i.e., the mean distance) on the	This method assumes that the
	to the environment may provide	configurations in the state space is a	– i.e. multiple metrics representing	scoring space of the input samples.	behavior of the SUT is deterministic
	big impact to the behavior.	measure of the similarity between the two	different types of properties are defined.		under one scenario configuration.
		scenarios.		The sampled scenarios are given to a	
				simulation platform. The simulation results	So far, the scenario model does not
		Covered layers: Not explicitly given. We		are evaluated according to the score space.	include reactive agents. The current
		assess that it should cover many of the			

		factors that may affect the decision-making		A clustering method is used to determine the	version is only for single agent
		module. The given case study uses		performance modes among the simulation	scenarios.
		an unmanned underwater vehicle as an		results.	Section 103.
		example, which cannot represent automated		resures.	It considers design of experiments
		vehicles.		performance boundary pairs are identified	(DOE) and test case generation as
		vernoies.		beside the boundaries between different	related domains.
				performance modes.	Telated dollians.
				performance modes.	Similar paper: [8] Nabhan2019a also
				Scenarios adjacent to the identified	uses learning based testing methods
				boundaries can be used as test cases.	to generate critical scenarios.
[9]	Activity: criticality check	The case study is a traffic jam approach	Criticality definition:	Input sce.: A given logical scenario	Required knowledge:
[9]	Phase: system verification and	scenario on a left-turned curved road with a	This paper interests in corner cases, where		Nehicle models in simulation
	system design (sensor range)	fixed radius of 50m. The ranges of three	small changes in the parameter value can	Output sce.: criticality	platform (CarMaker), which
	SOI: the whole system	parameters are defined and values are	trigger the change from a safety scenario	Process to train classifier:	
	<b>301.</b> the whole system	provided:	to a critical one. These corner cases are	Create a set of concrete scenarios by	provides training data and test data through simulation.
	This names proposes an approach	provided:			
	This paper proposes an approach to identify the performance	Fac yohiolo spood (40 70 km/h)	located around performance boundaries between critical scenarios and non-critical	sampling a given logical scenario with	A given logical scenario     Pre-defined criteria of criticality
		Ego vehicle speed (40 – 70 km/h)		specified sampling methods i.e., Monte	3. Pre-defined criteria of criticality
	boundary in the parameter space.	Target vehicle speed (5 – 20 km/h)	scenarios.	Carlo Simulation and Latin Hypercube (LHC).	Validation:
	Knowledge of performance	aperture angle of the radar sensor of the ego		· · ·	
	boundary helps to find corner	vehicle (10 – 25°)	In this paper, a scenario is considered as	2. Simulate the sampled concrete scenarios	The data acquired from simulation
	cases, which are located on the	l	critical when the ego vehicle cannot	to obtain simulation results (critical or	model is split into training set and
	performance boundary.	Covered layers by the case study:	prevent a collision in the simulation.	non-critical) as labels of the concrete	test set. The evaluation of the test
		Layer 4 + sensor configuration		scenarios.	set can prove the effectiveness of
				3. Use these data to train a Gaussian Process	trained model.
				Classifier (GPC) model, which yields the	It used a case study to validate the
				performance boundary.	estimation of the performance
				The current work focuses on the desired on	boundary. However, there are no
				The current work focuses on the derivation	validations on the criticality of the
				of a classifier that distinguishes critical	scenarios on the performance
				scenarios and non-critical scenarios. In the	boundary.
				future work, an adaptive framework will be	a
				integrated to conduct sampling on the	Similar paper:
				performance boundary to find corner cases.	[10] 8431291 uses GPC to identify
					safety boundary in the parameter
					space (i.e. collision or not). It
					proposes a criterion to evaluate the
					approximation quality of
					classification results and employs a

	Activity: Instantiation Phase: system verification SOI: the whole system	The term 'test scenario' is used without clear definition.	Critical test scenarios are defined as test	Input sce.: A given logical scenario	method to accelerate the boundary searching process.  Required knowledge:
	Phase: system verification			Input sce.: A given logical scenario	
	•	definition.	and a subject to the subject of the		neganica knowledge.
	<b>SOI:</b> the whole system		scenarios that contain critical behaviors	Output sce.: critical concrete scenarios	A logical scenario
			(e.g., hitting a pedestrian with high speed)		2. A simulator (PreScan)
l l	An automated testing algorithm that builds on learnable evolutionary algorithms to achieve the following goals: First, classification models guide the search-based generation of	In a motivation case study, it is described that 'scenarios capturing various road traffic situations and different pedestrian-to-vehicle and vehicle-to-vehicle interactions' and 'vary road-topologies, weather conditions and infrastructures.'	In this paper, criticality is evaluated on simulation results.  Critical regions are defined as the regions of a test input space that are likely to contain most critical test scenarios.	Critical scenario identification is formulated as a multi-objective search optimization problem and solved by Non-dominated Sorting Genetic Algorithm version 2 (NS-GAII). A feasible solution is a vector of values to input variables of the ADAS.	<ol> <li>Dynamic model of other road users</li> <li>Definition of critical behaviors (extracted from specifications)</li> <li>SUT (as black box)</li> </ol>
	tests faster towards critical test	Instead of explicitly defining 'test scenario', a	Critical behaviors: e.g., The main critical	Decision tree (DT) learning is used to learn a	Validation:
	scenarios.	related term 'test input space' (in our term, it	behavior of Automated Emergency Braking	classification model of critical behaviors.	A case study to show the exploration and exploitation of their searching
	Second, search algorithms refine	refers to the logical scenario or the scenario	(AEB) is extracted from the AEB		method.
	classification models so that the	configuration space) is used, which includes	requirements: "AEB detects a pedestrian in	NSGAII-DT generates critical test scenarios	
	models can accurately characterize	static input variables and dynamic objects. In	front of the car with a high degree of	and critical regions for ADAS.	Assumption: It is argued that for
	critical regions.	our understanding, these variables constitute the driving scenario.	certainty, but an accident happens where the car hits the pedestrian with a relatively	Subsequent search iterations are performed	testing at the system level, search-
	Aimed for improving effectiveness	the driving scenario.	high speed (i.e., more than 30km/h)". This	on the critical regions, generating and	based techniques are best suited.
	of the evolutionary search for large	Covered layers: 1,4,5	critical behavior refers to any AEB	evolving more critical test scenarios within	Decision trees is not used to predict
	and multidimensional input spaces.		simulation scenario exhibiting this behavior as a critical test scenario of AEB.	those regions using genetic operators.	whether a given ADAS scenario is critical or not. Instead, the decision
	It can be used in the system testing				trees are used: (1) to better guide
	phase. The purpose is to find				the search, and (2) to characterize
	critical regions in the simulation				the critical regions of the ADAS input
	environment.				space.
					Similar papers:
					[12] use genetic algorithm to detect
					critical scenarios for emergency
					braking function. It applies TTC as critical criteria. It also compares the
					effectiveness of finding critical driving scenarios with random searching.

[14]	Activity: Instantiation	The full scope of a logical scenario is not	Critical scenarios are defined as scenarios	Input sce.: A given logical scenario	[13] use genetic algorithm and simulated annealing respectively to detect critical scenarios for emergency function. It applies TTC as critical criteria. It also compares their performance in test parameter optimization with random searching
	Phase: system verification SOI: decision-making and control system  In this article, a generic simulation- based toolchain for the model-in- the-loop identification of critical scenarios is introduced. The proposed methodology allows the identification of critical scenarios with respect to the vehicle development process.  The toolchain is generic, but demonstrated using the example of automated highway chauffeur.  The investigated automated driving function is an SAE Level 3 highway chauffeur.  It can be used in system verification/ testing phase.	explicitly given in the paper.  In this paper, the scope of a scenario also includes disturbances (e.g., faults on the system, performance limitations and unexpected behaviors of other vehicles)  How these disturbances are introduced into the simulation is not mentioned in this paper.  Covered layers: 1,4,6 + possible faults and performance limitations (including the ones caused by extreme environmental condition)  The covered layers are judged by the proposed case studies.  Usually, the investigated time interval for traffic quality varies from several minutes to hours. In this paper, this time interval is too large and is adjusted to 15 s.  The spatial "domain of interest" (DOI) is chosen to be 450 m.	that need to be tested. The criticality of the scenarios is determined by both standard safety metrics and newly developed traffic quality metrics. A scenario is critical if any of safety metric or the overall traffic quality metric exceeds its threshold.  Standard safety metrics: 1. time to collision; 2. time to brake.  3. Introduced safety metrics: required deceleration (describes the deceleration of the ego-vehicle needed to generate a collision with 0 m/s)  The overall traffic metrics is a weighted sum of:  1. traffic density (macroscopic description)  2. the velocity deviation divided by the velocity mean value of the ego-vehicle as an indication of the microscopic traffic quality  3. Close-range interactions. (nanoscopic)  4. Speed change of the ego vehicle (individual metric)  The weights are optimized by training data (labeled by experts)	Output sce.: critical concrete scenarios  The identification process is realized by a coupled simulation framework combining a vehicle dynamics simulation, a traffic simulation and a cooperation simulation.  The behavior of other traffic participants, like defensive or aggressive, is considered in the traffic simulation environment.  According to our understanding, the parameters in the logical scenario are randomly sampled.  For identification and evaluation of critical scenarios, the corresponding thresholds for the criticality classification are specified, including three safety metric values and an overall grade.	1. A logical scenario 2. Simulators (traffic simulation, vehicle dynamic simulation) 3. Dynamic model of other road users (in the traffic simulator) 4. Metrics and thresholds for criticality 5. SUT (as black box) 6. Expert experience to label the overall traffic quality metric.  Validation: A case study is used to show the applicability of the approach.  Limitation (assumption of a constant-velocity model): One of the major issues for the dynamic coupling between traffic and vehicle dynamics simulation is the discrepancy of sample time. Therefore, the absent motion of the traffic participants provided by the traffic simulation is predicted with a constant-velocity model.
			Each metric has its own domain of interest (DOI).		

[15]	Activity: Formalization (including	The input logical scenario is described by a	The criticality of a scenario is evaluated by	Input Sce.: a Logical scenario (a pre-defined	Required knowledge:
-	quantification) & Instantiation	predefined hierarchical ontology, which	its complexity.	ontology of scenario description)	A predefined scenario description
[17]	Phase: System verification	includes (1) environment, e.g., weather,		Output Sce.: a set of concrete scenarios	ontology
and	<b>SOI:</b> the whole ADAS system	time, road; (2) self-state, e.g., speed and	Each leaf factor in the scenario description		The relative importance of the
[18]		(3) Other traffic participants' state, e.g., Road	ontology has discrete values. Each value	Process:	values under each leaf factor in
	This paper presents an automatic	congestion. The leaf nodes of this ontology	has an importance index (a real number)	Given the relative importance of the	the topology
	test scenario generation method,	are the possible values of the scenario	according to its potential influence on the	values under each leaf factor, the	<ul> <li>Simulator (PreScan)</li> </ul>
	which is based on combinatorial	description parameters.	performance of the SOI. The complexity of	contribution of each factor or value to the	
	testing.		a concrete scenario is indicated by the sum	complexity of the whole scenario can be	Validation:
	When generating test scenarios,	A detailed table of these parameters is	of the importance indexes of all the values	determined by the Analytic Hierarchy	By comparing with other
	besides combinatorial coverage,	presented in the papers.	in the vector (i.e., the concrete scenario).	Process (AHP).	combinatorial test case
	they also maximize the complexity		The importance indexes are determined by	A covering array generation algorithm is	generation methods, the
	of the generated scenarios.	The value of each parameter is discretized.	expert knowledge.	proposed to guide the test case	proposed method generates
	The scenario complexity is defined	A concrete scenario is a vector of the values		generation method to maximize the	more complex scenarios with
	based on the influence of each	of all the leaf nodes of the hierarchical		complexity of the scenarios in the	acceptable number of total test
	scenario factor on the performance	ontology.		generated covering array.	cases to guarantee combinatorial
	of the SOI.	Covered laverer 1 A F		The generated test scenario is constructed	coverage.
		Covered layers: 1, 4, 5		into simulation models.	Simulations in PreScan are used
					to show (as a proof of concept)
					that more complex scenario
					indicates higher failure rate.
[19]	Activity: Formalization (derive the	Parameters to sample in the example cut-in	The proposed method tries to find	Input Sce.: Logical Scenario	Required knowledge:
	distributions of parameters) &	maneuver scenario:	common and risky scenarios.	Output Sce.: a set of concrete scenarios	Dynamic model of certain use
	Instantiation	Speed of following/merging vehicle	Criticality definition: In this paper, risk	Th	case(scenario)
	Phase: system verification	Max acceleration of merging vehicle	index is used to represent criticality.	The generation of concrete scenarios	Naturalistic driving data
	SOI: decision-making and control	Lateral/longitudinal distance	Minimum TTC is set as risk index in the cut-	includes 3 steps:	Well-defined risk indices
	system	Lateral speed of merging vehicle	in maneuver example. The definition of minimum TTC is not explained in the paper.	Step 1 is to build the kinematic model for	
	The purpose of this method is to	Bisasilis at a second above	minimum ricis not explained in the paper.	automated driving function and get the	Validation:
	analyze naturalistic driving data	Distributions of these parameters are	The identified scenarios are Safety critical	parameter sets.	In a cut-in maneuver case study, the
	(NDD) and generate critical test	derived from NDD.	for generic AD systems.	Step 2 is to generate Gaussian mixture	proposed method identifies that the criticality is statistically related to
	cases for safety evaluation for AD	Scenarios: In the given example (the cut-in	Tor generic AD Systems.	model (GMM) model to analyze the	the lateral (de)acceleration and the
	vehicles.	maneuver), scenario is the kinematic	In result analysis and validation part,	distributions for parameters using	cut-in duration. However, this
		behaviors of following and merging vehicles	critical regions are identified. In the cut-in	naturalistic driving data.	finding is not further validated.
	The novel idea is to involve risk	incorporating with the risk indices, based on	maneuver example, scenarios with short	Step 3 is to perform parameter sampling	initialing is not further valuated.
	indices to constrain the sampling	a cut-in maneuver on an expressway.	cut-in duration and high lateral	based on (Markov chain Monte Carlo) MCMC	
	process, so as to find the critical	a sac in maneaver on an expressival.	(de)accelerations are identified as the	method, the sampling can be performed with	
		Covered layers: Layer 4	critical region.	and without the consideration of risky index.	
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Configuration space.   Since the sampling also considers the distributions of the parameters, commonality of the scenario is also part of the criticality definition, since the sampling considers the distributions of the parameters.		ragions on the scenario	I	1	When considering the risk index, it will be	
Activity: Instantiation   Activity: Instantiation   Soi: AbS system verification   Soi: Abs		_		Cinco the compling also considers the	1 · · · · · · · · · · · · · · · · · · ·	
Activity: Instantiation   Covered layer:   In the case study scenarios   Sampling considering the risky index will show the distribution of risky scenarios on the scenario configuration space.   Sampling considering the risky index will show the distribution of risky scenarios on the scenario configuration space.   Sampling considering the risky index will show the distribution of risky scenarios on the scenario configuration space.   Sampling considering the risky index will show the distribution of risky scenarios on the scenario configuration space.   Sampling considering the risky index will show the distribution of risky scenarios on the scenario configuration space.   Sampling considering the risky index will show the distribution of risky scenarios on the scenario configuration space.   Sampling considering the risky index will show the distribution of risky scenarios on the scenario configuration space.   Sampling considering the risky index will show the distribution of risky scenarios on the scenario configuration space.   Sampling considering the risky index will show the distributions of the scenario configuration space.   Sampling considering the risky wheth distributions of the scenario configuration space.   Sampling considering the sampling considering the space of considering the sampling considering the space of sampling considering the space of sampling considering the space of sampling con		configuration space.			used as a constraint for the sampling.	
the criticality definition:  [20] Activity: instantiation Phase: system verification SOF: ADAS system Phase: system verification SOF: ADAS system Phase: system verification SOF: ADAS system verification SOF: ADAS system Phase: system verification SOF: ADAS system					Sampling considering the ricky index will	
Considers the distributions of the parameters.   Considers the distributions of the parameters.   Critically definition:   In the case study scenario, acceleration, SOR: ADAS system   Computation   SOR: ADAS system   Computation   SOR: ADAS system   Critically definition:   In the case study scenario, acceleration, speed, moving trajectory and obstacle detection ability of the vehicle are listed but seem that such asset of parameter parameters prace based on surrogate model and stochastic optimization.   Surrogate model and stochastic optimization.   Surrogate model and stochastic optimization.   Surrogate model is used in optimization to reduce computational cost.   Comp				1	, , ,	
Covered layer:   In the case study scenario, acceleration, Soft-ADAS system   This paper proposes a method to identify faulty behavior regions in the scenario parameter space based on surrogate model and stochastic optimization.   Surrogate model and soft optimization to reduce computational cost.   Surrogate model cost used in optimization to reduce computational cost.   Surrogate model is used in optimization to reduce computational cost.   Surrogate model is used in optimization to reduce computational cost.   Surrogate model is used in optimization to reduce computational cost.   Surrogate model is used in optimization to reduce computational cost.   Surrogate model is used in optimization to reduce computational cost.   Surrogate model is used in optimization to reduce computational cost.   Surrogate model is used in optimization to reduce computational cost.   Surrogate model is used in optimization to reduce computational cost.   Surrogate model is used in optimization to reduce computational cost.   Surrogate model is used in optimization to reduce computational cost.   Surrogate model is used in optimization to reduce computational cost.   Surrogate model is used in optimization to reduce computational cost.   Surrogate model is positive to the local minimum to cation (the result of the optimization by a compared with those on surrogate model is positive to the simulation in the simulation is defined by time or collision speech.   Surrogate model is positive to the local minimum ocation (the result of the optimization by a compared with those on surrogate model is compared with the optimization by a compared with those on surrogate model is compared to prove the effectiveness of the method.      Surrogate				_ · · · · · · · · · · · · · · · · · · ·	1	
Activity: Instantiation   Phase: system verification   SOI: ADAS system   Country					the scenario configuration space.	
Phase: system werflication SDI: ADAS system This paper proposes a method to identify faulty behavior regions in the scenario parameter space based on surrogate model and stochastic optimization.  Surrogate model is used in optimization to reduce computational cost.  Surrogate model is used in optimization to reduce computational cost.  The specific model considerable and stochastic optimization to reduce computational cost.  The specific model considerable and stochastic optimization to reduce computational cost.  The specific model considerable and stochastic optimization to reduce computational cost.  The specific model considerable and stochastic optimization to reduce computational cost.  The specific model considerable and stochastic optimization to reduce computational cost.  The specific model considerable and static obstacted life the governing that the governing that the specific model is used in optimization to reduce computation to reduce comp	[20]	A etivitus Instantiation	Covered lever	<u>'</u>	Immut Con a Logical Connexio	Dogwined knowledge:
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detection ability of the vehicle are listed but set with fixed number, 2-D position of static obstacle is the only variable in the search space (maybe layer 4).  This paper proposes a method to identify faulty behavior regions in the scenario parameter's space based on surrogate model and stochastic optimization.  Surrogate model is used in optimization to reduce computational cost.  Surrogate model is used in optimization to reduce computational cost.  Surrogate model is used in optimization to reduce computational cost.  This paper proposes a method to identify faulty behavior regions in the scenario sale observed on surrogate model and stochastic optimization.  Surrogate model is used in optimization to reduce computational cost.  This paper latks about testing scenarios.  This paper talks about testing scenarios.  This paper talks about testing scenarios.  This paper talks about testing scenarios.  detection ability of the vehicle are listed but dobtance in the search when a collision of static obstacle (if there is no collision) or the collision (TTC) value between vehicle collision (TTC) value between vehicle and static obstacle (if there is no collision) or the collision speed. The scenario will be more severe if the govehicle crashes at higher speed.  Sead on the surrogate model solutility with Radial Basis Function approximation and it is trained in each iteration.  Sender of the cost function and estimate the result of the cost function and the cost function and estimate the result of the cost function and the cost function and estimate the result of the cost function and the cost fun			1		Output sce.: a set of concrete scenarios	
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Phase: system validation	[22],	Assessment		defined based on safety and functionality	Input Sce.: A logical scenario	A given logical scenario
		Phase: system validation				

[23],	SOI: the whole system	The scenario model does not specify the	(if the ego-vehicle can complete the driving	Output Sce.: a library of critical concrete	2. Predefined KPIs (e.g., mnpETTC)
[24]	The purpose of this work is to generate a library of critical testing scenarios for connected automated vehicles. This method targets to find common and challenging scenarios. Scenarios in the library are critical for most of the AVs.  Scenarios within this library will be	duration of a scenario.  When generating critical scenarios, vehicle behaviors are represented by surrogate models, e.g., polynomials.  Covered layers: The surrogate model only considers layer 4.	task).  The scenario generation process is to find common and challenging scenarios. Challenging level is quantified as mnpETTC (a variance of TTC). The commonality is quantified as the distance (on the scenario configuration space) between the scenario and a high exposure frequency zone (i.e.,	scenarios  The scenario searching process is formulated as a two-step optimization problem. The decision variables are the parameterized scenario configurations of interest (normally referring to what can be changed in the given logical scenario e.g., the parameters of the dynamic objects). An example in this paper for a cut-in scenario is the cut-in distance	3. A Surrogate model to fast compute the KPI 4. Naturalistic Driving Data (to determine the distributions of the parameters of the logical scenario)  Validation:
	randomly sampled as an importance sampling method to estimate the accident rate and failure rate. The sampled scenarios		<ul><li>Ω) in Naturalistic Driving Data (NDD)</li><li>(e.g., 95% percentile)</li><li>For the evaluation with importance</li></ul>	and the speed difference with the vehicle in front. The objective function represents the criticality definition. Constraints are used to define the ranges of the parameters.	They compared the failure rate estimated by their method with the failure rate measured from simulation/real testing.
	will be used as test cases in an augmented reality testing environment, where the egovehicle runs in the real world and receives other vehicles' information from a simulated environment. In other words, other vehicles are simulated, and their information is sent to the egovehicle through I2V.		sampling phase, the metric (after testing) for safety is the accident rates; and the metric for functionality is the failure rate.	The first step of the optimization tries to find multiple local optimal solutions with a multistar optimization method (there is no simulation involved). The second step tries to search the neighborhood of the local optimal solutions to find all the scenarios whose criticalities are within a given threshold.  If design variables contain profiles (e.g., acceleration profiles in one of the case studies), reinforcement learning is applied.  [24] applies an adaptive method to change the importance distribution based the test	This paper has some arguments on which parameters should be fixed and which should be variable (in this paper, these variables are called design variables)  Similar paper: [25] uses real field test data and applies importance sampling method to accelerate the testing process and achieve the full coverage test.
[26]	Activity: Instantiation & assessment Phase: system validation SOI: decision-making and control system The proposed method in this paper is to validate the failure rate of an ADS via importance sampling. It	In this paper, a scenario is defined as a combination of the actions of the ego vehicle, the static environment (e.g. infrastructure and weather), and the ongoing activity of the dynamic environment (including the other traffic participants) for a certain period of time.	In this paper, criticality is defined based on KPIs and the corresponding thresholds. TTC is used in its example. In the case study, critical scenarios are those whose TTC belongs to the 5% lowest.	results.  Input Sce.: Logical Scenario Output Sce.: a set of concrete scenarios  The main purpose of this method is to evaluate the failure rate of the ADS. It can also generate critical scenarios for testing.  It has the following steps.	Required knowledge: 1. A logical scenario 2. Surrogate model based on vehicle dynamics to calculate the indicators (TTC) 3. Metrics for criticality

	can also fasten the speed to find critical scenarios.	Covered layers: 1, 2, 4, 5		<ol> <li>Monte Carlo simulation is used to find a set of critical scenarios (whose TTC belongs to the 5% lowest). The distributions of the scenario parameters are derived from real-life data by kernel density estimation (KDE).</li> <li>Approximate the importance sampling density function on the parameter space of the critical scenarios achieved from step 1.</li> <li>Use this density function for the importance sampling to get more critical scenarios and to get a more precise estimation of the failure rate.</li> </ol>	4. Distribution of scenario parameters from Naturalistic driving database 5. Simulator (Simulink)  Validation: They use a car-following scenario as an example. The generated test cases are given to a simulator (MATLAB + Simulink) and compare the result between the proposed method (important sampling) and normal Monte Carlo Simulation.
[27]	Activity: Instantiation Phase: system verification SOI: decision-making and control system  The proposed method characterizes the deer model as the traffic participant, reacting with a startle response when a vehicle is approaching. Ego vehicle behavior is simplified into four rudimentary modes with different reactions after detecting deer. Genetic Algorithm (GA) is applied to optimize parameters in deer motion model, which helps to explore worst case interaction (collision) between deer model and vehicle.	In this paper, a scenario is constructed mainly with 3 phases in deer road crossing event, which are initial acceleration, deceleration and turn and final acceleration. Each phase is modelled with step response of transfer function. Parameters exist in the deer reaction model to describe its trajectory, including deer initial angel, acceleration phase time, time constant in transfer function and maximum speed. The only variable for ego vehicle is the number of 4 different pre-defined driver modes.  Covered layers: 4	In this paper, criticality is defined with minimum distance between a deer and the ego vehicle.  The proposed method in the paper can be applied for generic AD function since predefined driver reaction modes are specified.	Input Sce.: Logical Scenario Output Sce.: a set of concrete scenarios  Implementation:  1. Design deer motion model and define driver reaction modes (e.g. swerve, brake, hybrid and no reaction).  2. Perform optimization with Genetic Algorithm to identify most challenging scenarios.	Required knowledge:  1. Relevant biological information for deer model setup.  2. Defined driver reaction strategies.  Validation:  Case study shows validity of proposed method and comparison is discussed about different performance with variant vehicle reaction.
[28]	Activity: Criticality check Phase: system verification SOI: decision-making and control system	The scenario in this paper is described by the specified term situation and episode. A situation (scene in our terminology) is a single moment with information about all traffic participants, and episode (scenario in our terminology) represents the changes	In this paper, critical scenario is evaluated by criticality index, which calculates critical situations over the episode. Each situation can be evaluated with a criticality value from 0 – 1. In case study, a threshold is set	Input Sce.: Logical Scenario Output Sce.: a classifier in situational space Implementation: 1. Design vehicle dynamic model with parameter ranges and distributions.	Required knowledge: 1. Vehicle dynamic model 2. Real-world data for validation 3. Matlab as simulator Validation:

	The proposed method designs a classifier to examine critical scenarios in situational space. The classifier is achieved with support vector machine. Real world data in defined situational space is recorded and used for validation.	over time of the underlying situation, which contains trajectory details of all related vehicles. Relevant parameters for vehicle dynamic model include velocities and positions for ego and other vehicles.  Covered layers: 4	to classify critical scenarios from non-critical ones.	Conduct sampling twice with different group sizes to generate training dataset and test dataset. Criticality of each scenario is labelled through simulation.     Train SVM and evaluate the performance.	This paper analyses performance of the proposed method by processing 24 hours of driving sequences to generate a real-world dataset for validation.  This paper applies simulation data for training and real test data for validation. The performance of predictability is validated.  Similar papers:  [29] uses SVM to identify critical scenarios under cut-in situation.  THW (time head way) and relative velocity are critical criteria.
[30]	Activity: Instantiation Phase: system verification SOI: the whole system (ADAS)  This paper proposes a method to generate test scenarios for ADAS function. The proposed framework supports hardware-in-the-loop and test automation. Functional coverage is examined in the method to check how much testing has been completed against defined use case requirements.	In this paper, a scenario is the combination of test scenario and test case. A test scenario refers to the simulation environment, including other traffic participants and weather conditions. And in test case, actions by driver (human maneuver such as stepping on accelerator and braking) is specified. The target function in this paper is ADAS function (AEB in case study), which requires driver operations to trigger function. For this reason, the driver action is quantified with brake pedal value and accelerator pedal value.  Covered layers: 4, 5 + driver behavior	In this paper, criticality for scenario is defined as if longitudinal collision occurs.	Input Sce.: Logical Scenario Output Sce.: a set of concrete scenarios  Implementation:  1. Perform randomization on scenario space and driver behaviour space. Set up HIL interface and start simulation in an automatic manner to search critical scenarios.  2. Check functional coverage metrics. The coverage metrics are calculated and evaluated in Vitaq, the test automation tool. Coverage is achieved by partitioning parameters values in sub-ranges and conducting simulation in each range with required number of tests.	Required knowledge:  1. Hardware preparation including ECU with target ADAS function and hardware-in-the-loop test environment  2. Tool for test automation and randomization  3. Simulator Validation: This paper is in the absence of validation part.
[31]	Activity: Instantiation Phase: system verification SOI: decision-making and control system This paper proposes a method to analyze the criticality of a certain	In this paper, a multi-level approach for safety consideration is proposed. The scenarios are divided into frequently occurring scenarios, less frequently occurring scenarios and scenarios beyond the crash boundary. The latent crashes happening in the first two types of scenarios can be	In this paper, criticality is evaluated based on Abbreviated Injury Scale (AIS) methodology. A lookup table is used to match contact velocity in both front-end crash and rear-end crash with injury probability for MAIS 2+. A threshold is set to evaluate whether the resulting risk is	Input Sce.: Logical Scenario Output Sce.: a set of concrete scenarios Implementation: 1. Build crash model and define logical scenario.	Required knowledge:  1. Vehicle dynamic model and simulation environment  2. Correlation between simulation results and crash severity level.  3. Real traffic measurement for driving behavior derivation

	virtual-simulated scenario and therefore define crash boundary in the parameter space. The focus of this paper is the criticality check for concrete scenario from a given logical scenario.	handled by ADAS/AD function and they are considered at design stage. The evaluation of scenarios beyond the boundary reveals edge cases and is referred to as 'beyond-design-basis safety assessment'. In the scenario, vehicle braking behavior is specified and fitted from real traffic measurement. Parameter ranges are specified based on statistical information from real-world measurements.  Covered layers: 4	acceptable or not. Through a full-scale grid search in parameter space, critical scenarios can be found, and crash boundary is identified. Crash boundary separates safe conditions from unsafe ones based on estimation of risk probabilities. Its location is decided by the defined threshold.	<ol> <li>Setup corresponding relationship between simulation results and injury risk probability.</li> <li>Perform a grid search with simulation in parameter space and evaluate injury risk level.</li> <li>Obtain crash boundary using threshold of acceptable crash probability.</li> </ol>	4. CarMaker  Validation:  This paper applies ACC with autonomous overtaking function as a case study. The crash boundaries of ego vehicle and front vehicle are analyzed.
[32]	Activity: Instantiation Phase: system verification SOI: Control part of a Lane keeping system, excluding perception  This paper presents an approach to generate test cases and expose safety-critical problems with AsFault. It focuses on the generation of road topology by procedural content generation and create critical scenarios by search-based testing.	In this paper, the scenarios are constructed with ego vehicle equipped with lane keeping functionality (SUT) and road network.  Scenarios for testing is derived by combining different road segments and forming road networks with AsFault prototype, which uses genetic algorithm to iteratively refine road networks.  Road network generation method in this paper ensures the validity of the generated road (gapless and non-self-intersecting) and specifies properties with regards to length, curvature and intersection locations.  Segments of road: defined by back line (starting part of segment) and front line (polyline which defines angle and length of segment).  Road network: generated by combination of roads, only feasible when intersection point of central polylines for different road occurs.  Covered layers: 1	In this paper, a scenario is viewed as critical when the distance between the position of the ego-car and the center of the lane was bigger than the half of the lane width.	Input Sce.: a logical scenario Output Sce.: a set of critical concrete scenarios  Implementation:  1. Generate road network with procedural content generation method.  2. Simulate and evolve road networks by AsFault with various search operators (e.g., road mutation, join crossover and merge crossover) through replacing or combining road segments to generate road network and find critical scenarios for Lane Keeping function. When an invalid road network is found, the combination will be aborted. Constraints are not used because 'generate and validate' scheme proves efficiency in this study.	Required knowledge:  1. AsFault as test cases generation platform for road topology creation by procedural content generation.  2. Simulator, BeamNG.research  3. Search operators to mutate and recombine roads.  Validation:  This paper uses Lane Keeping function as a case study to evaluate the performance of proposed method. Two different control algorithms are implemented, and results are compared.

[33]	Activity: Instantiation	The derivation of a search space is not	In this paper, scenarios are critical when	Input Sce.: a logical scenario of a particular	Required knowledge:
	Phase: system verification	discussed in this work. In the paper, it is said	they are near-collision and collision cases.	scenario type	1. Fitness functions
	<b>SOI:</b> not clear, use case is a	that OpenScenario or CommonRoad format	Criticality is checked by fitness functions.	Output Sce.: a set of near-collision and	2. Optimization tool
	highway traffic system	can be used. The paper takes use of scenario	This paper proposes several different	collision concrete scenarios of one particular	3. Simulator
		types defined in [34], where scenarios are	templates to construct the fitness function	scenario type	Validation:
	This paper proposes a method to	grouped into 24 types. This paper analyzes 2	for scenario search. Each template is a		This paper is in the absence of
	build templates for formulating	types of them as case studies. The use case	specification from one perspective. Fitness	Implementation:	validation part.
	fitness functions in order to test AD	in the paper, highway traffic system, only	function is constructed by combining these	1. Create templates. They can be used for	
	system and generate worst-case	covers layer 4.	templates. Fitness functions can be	different primitive qualitative and	
	scenarios. The fitness function is		classified into two categories: 1) testing	quantitative test goals.	
	used as constraints in searching	Action of ego vehicle is considered in the	against safe operating envelopes (e.g., the	2. Combine templates to generate fitness	
	and can be combined in the	scenarios, for example, ego vehicle must do	distance between the ego vehicle and	function so that it can be used for complex	
	application of multi-objective	lane change and then follow certain distance	another vehicle) and 2) ensuring	scenario searching.	
	searching for complex scenarios.	constraints with other vehicles. These	qualitative test goals (e.g., if an event	3. Search for the violation of test goals with	
		conditions are formulated into fitness	happens at the right moment). The non-	fitness functions in the prescribed search	
	The derivation of fitness function is	functions.	fulfilment of qualitative goal is assigned by	space by simulation. The search engine	
	the focus of this work, while how to		the measurement of how far it is away	and simulator are not described in the	
	perform searching in a certain	Covered layers: 4 (including the intention of	from goal, which can be transformed and	paper.	
	scenario type with a given fitness	the ego vehicle)	viewed as a quantitative way. The		
	function is not described in detail.		combination of fitness functions can be		
			used in single-objective search and multi-		
			objective search for complex scenarios.		
[35]	Activity: scenario variation and	In this paper, scenario is defined as a timely	In this paper, the criticality of a scenario is	Input Sce.: FOT/NDS data of a critical	Required knowledge:
	criticality check	series of scenes. Scene is the snapshot in	evaluated by risk based KPI. In the case	concrete scenario	1. FOT/NDS data of the
	Phase: system verification	time, containing static and dynamic	study, time-to-react (TTR) [36] of every	Output Sce.: a set of critical concrete	corresponding critical functional
	SOI: decision-making and control	properties in the environment.	scene is calculated and mapped to risk	scenarios around the given scenario	scenario
	system	JSCEN, proposed scenario description	probability by a weighting function. The		2. JSCEN scenario format
		method, is used in the paper to characterize	risk of a scenario is then represented by	Implementation:	3. Simulator to evaluate scenario
	This paper proposes a method to	scenarios. It provides information of starting	the maximal risk value of the scene.	Extract a set of particular critical scenarios	criticality
	evaluate criticality of a scenario	positions and driven traces for all traffic		with the same maneuver (e.g., right lane	4. Risk probability mapping to
	through risk based KPIs and	objects, including ego vehicle.		change) and perform feature selection.	evaluate risk of scenarios based
	generate new test scenarios by			2. Use principal component analysis (PCA) to	on simulation results. (e.g.,
	variation through PCA. The	Covered layers: 4		segment scenarios into a lower-	weighting TTR values into risk
	generated scenarios are similar to			dimensional component space.	values)
	the original ones, with respect to			3. On the component space (the output of	Validation:
	trajectories, maneuver behaviors			PCA), conduct component variation. (i.e.,	This paper uses a cut-in and brake
	and risk evaluation results, which			adding noises to each dimension of the	scenario as the case study. Risk of
	help to provide relevant scenarios			component space)	NDS data is evaluated and scenario
	from naturalistic data and add				variation is used to generate more

	additional test cases in function assessment process.			4. Perform reverse transformation and concatenate with other scenario segments which are not variated to form a completed scenario.  5. Fit the scenario into JSCEN format to generate variated scenarios.  6. After the generation of scenarios, perform criticality evaluation with risk based KPI through simulation.	scenarios. The risks of generated scenarios are also evaluated to show their relevance to the original scenarios.
[36]	Activity: criticality check (risk assessment) for a given concrete scenario Phase: system validation SOI: decision-making and control system  The paper proposed an approach to measure the criticality of a given driving scenario fitted on the requirements of safety testing: (1) no false negatives (i.e., critical scenarios that are predicted to be non-critical); and (2) less false positives.  Multiple possible scene evolutions were simulated via Monte-Carlo simulation together with their probabilities of occurrence.  Monte-Carlo simulation here means multiple simulations.	A scenario is a series of scenes connected by time.  A scene is defined as an instance in a parameter space, which contains the position, speed, acceleration, heading and heading and turning angle of the ego vehicle and other traffic objects.  A concrete scenario configuration is the configuration of the initial scene. (implicit)  Covered layer: 4	This paper proposes a method to estimate risk for a particular scene. The risk of a scenario is determined by the highest scene risk.  The risk of a scene is defined based on the severity and the probability of occurrence of a crash.  The severity is estimated by time-to react (TTR) of the ego vehicle. The probability is estimated through a Monte-Carlo simulation.  TTR describes the time which is left to avoid the collision within the physical constraints of the vehicle. It is the maximum value among time-to-steer (TTS), time to brake (TTB) and time to kickdown (TTK).  The calculation of the TTR value itself is done by iterating stepwise through time, calculating paths for full left and right steering, full braking and accelerating and checking if the calculated trajectories avoid the collision.	<ol> <li>Input Sce.: a concrete scenario</li> <li>Output Sce.: the risk of the concrete scenario</li> <li>How the Monte-Carlo simulation is conducted:</li> <li>The behavior of other traffic objects is modeled with a simple Constant Turn Rate and Acceleration (CTRA) model. The parameter distributions in the CTRA model are achieved from naturalistic driving data.</li> <li>The scene under evaluation is used as the initial scene. Its development over time is predicted within a given prediction horizon.</li> <li>Within the prediction horizon, the trajectory of the ego vehicle is planned (at the beginning) with its trajectory planning algorithm. For each traffic object, a given number of possible trajectories are predicted with their possibility calculated.</li> <li>TTRs are calculated for each trajectory pair (one from the ego vehicle and one from a traffic object).</li> <li>A risk value (between 0 and 1) is calculated according to all the TTRs and the probability of the corresponding trajectory of the traffic object.</li> </ol>	Required knowledge:  1. CTRA model  2. Naturalistic driving data (euroFOT)  3. Predefined parameter for the Monte-Carlo simulation: prediction horizon, prediction step, number of predicted trajectories per traffic object, point of no return (if TTR is below this point, the risk will be 1), maximum risk time (if TTR is larger than this, the risk will be 0), weighting slope (a coefficient to corelate RRT and the risk value) and consolidation threshold (this is used when multiple vehicles are involved in the scenario. Detail explanation can be found in the paper).  Validation:  This paper uses a case study to verify the applicability of the method.
[37]	Activity: formalization and instantiation	In this paper, scenarios can be described in three levels, which are use case, test	In this paper, the critical criterion, as the optimization objective, is derived and	Input Sce.: a use case as functional scenario	Required knowledge:

	Phase: system verification SOI: decision-making and control system  This paper presents a method to find multiple critical scenarios in a set of test cases, which are derived from a use case. The method focuses on the improvement of Bayesian optimization algorithm to identify minimal points in multiple regions by iteratively searching.	scenario and test case, corresponding to functional scenario, logical scenario and concrete scenario in our terminology. The logical scenario is derived through the analysis of description of ego vehicle, together with its goals, activities and environment. The three levels of scenarios follow a pyramid structure. A use case can have multiple test scenarios and even more test cases. For example, a use case can be a pedestrian crossing road when ego vehicle reducing its speed. Test scenarios for this use case specify dynamic elements (e.g., pedestrian behavior) and test cases are generated with concrete values (pedestrian speed).  Covered layers: 4	formulated from Systems Theoretic Process Analysis (STPA). Scenarios are critical if the collision occurs between pedestrian and ego vehicle. The objective function in the case study is to minimize the longitudinal and lateral distance between the car and pedestrians.	Output Sce.: a set of critical concrete scenarios  Implementation:  1. Use STPA to identify test scenarios. With the application of STPA, critical criteria and searching objective are also obtained.  2. Perform Bayesian optimization to find minimal points. Search the minimum in the space and eliminate its local region afterwards with a predefined size. Each dimension in the space will then be divided into two new regions as upper and lower search region.  3. Continue the process iteratively until all regions containing a minimum are identified.	1. Use cases for derivation of scenarios 2. Carmaker 3. Optimization tool Validation: This paper applies the proposed method on a SAE Level-4 Low Speed Automated Driving system as a case study to evaluate the performance. Multiple test cases are identified, which validates the applicability of the method.
[38]	Activity: Criticality check Phase: design and calibration SOI: decision-making and control system  This paper proposes a method to estimate collision probability between a vehicle and an obstacle in a scenario. Collision probability is calculated based on existing trajectories of the ego vehicle and the obstacle. The results of collision probability will then be applied in the calibration of a controller.	Scenario contains trajectories and bounding boxes of the ego vehicle and the obstacle. Trajectory includes midpoint location of the rear end and orientation.  Covered layers: 4 (including the possible behaviors of the ego vehicle)	In this paper, criticality is defined as the estimated probability of collision for a trajectory. With uncertainties in environment, there will always be a possibility of a collision. For each scene, Monte Carlo simulation is used with probability density function of the possible trajectories of the ego vehicle and the obstacle to calculate if they overlap in every possible situation. In the end, collision probability is represented with its value at each time step.	Input Sce.: a concrete scenario, size of vehicles, PDFs of waypoints of the trajectories Output Sce.: estimation of collision probability at each time step  Implementation: The method calculates collision probability by applying Monte Carlo simulation with position probability density functions of ego vehicle and obstacle in each simulation step, in order to check the proportion of overlapping. It will be evaluated iteratively with different parameter/threshold values and used in the application of calibration.	Required knowledge:  1. probability density functions of position for ego vehicle and obstacle  Validation:  This paper applies Lane Change Assistance System as a case study to evaluate the performance of the proposed method. Two different thresholds are set to demonstrate the calibration process. Their resulting collision probabilities are compared.
[39]	Activity: Criticality check Phase: system verification SOI: decision-making and control system	The scenario is built up with system dynamic model of ego vehicle and other traffic participants (e.g., static obstacle and other vehicles). System dynamic model specifies	In this paper, criticality is defined by criticality metrics, which is formulated by objective function in MPC. By optimizing the trajectory in a scenario, an optimal trajectory is reached. The criticality is	Input Sce.: a logical scenario (trajectory to be optimized) Output Sce.: criticality of the scenario Implementation:	Required knowledge:  1. a logical scenario 2. optimization toolbox in MATLAB 3. a specific AD system

					<u>,                                      </u>
	This paper presents a method to assess a scenario with criticality metrics. The metric is calculated based on optimization of a defined criticality in MPC application for trajectory control. Four scenarios for highway traffic are evaluated and a parameter variation is conducted to analyze effects of parameters in the system dynamic model.	the position, velocity, acceleration, and yaw angle of the vehicle.  Covered layers: 4	denoted by the objective function value of the optimal trajectory.	<ol> <li>Describe system dynamics with state space model. Define objective function and constraints. The objective function is regarded as a criticality metric.</li> <li>Define test scenarios.</li> <li>Execute optimization with MPC to optimize trajectories for scenarios and estimate criticalities.</li> </ol>	4. criticality metrics Validation: This paper applies four scenarios that are typical for highway traffic to evaluate their criticality with criticality metrics
[40]	Activity: Formalization and instantiation Phase: system verification SOI: The act component (control algorithm)  This paper presents an approach to generate test cases through search-based testing (SBT) in AD control application. Three industrial use cases, ACC, lane-keeping and steering control, are described in the paper, where the steps of specification analysis and critical scenario generation are studied. This paper also presents lessons learnt from the successful applications of SBT.	In the paper, scenario is initially described in a linguistic way with requirements. Scenario description is translated to test setup and specification is translated into system temporal logic in falsification tools (Breach and S-TaLiRo). For different scenarios, included parameters are in different aspects. In general, this paper considers vehicle parameters (e.g., velocity and distance), environment parameters (e.g., velocity of wind affecting the vehicle) and road parameters (e.g., slope and curvature).  Covered layers: 1, 4, 5	In this paper, a scenario is critical if it violates requirements from STL specification. Regarding case studies presented in the paper, criticality is identified with too close distance between vehicles.	Input Sce.: a scenario description Output Sce.: a set of critical concrete scenarios  Implementation: 1. Analyse scenario requirements and build STL for specifications. 2. Select parameters. 3. Perform SBT with Bayesian optimization and detect critical scenarios.	Required knowledge:  1. scenario description (functional)  2. Specifications for criticality definition  3. simulation tools (MATLAB)  Validation: This paper applies three use cases in an industrial AD setting to demonstrate the application of SBT.
[41]	Activity: Instantiation Phase: system verification SOI: Decision-making and control system (AD general)  This paper proposes a rule-based algorithm to detect critical scenarios in the parameter space. The algorithm will select the driving behavior of other vehicles to	In the paper, scenario is defined with behaviors of the ego vehicle and other vehicles. The go point of the ego vehicle is specified to give the final target. The initial position, speed, acceleration and lane change behavior are specified and discretized. At most 5 vehicles can drive on the road.  Covered layers: 4	In this paper, a scenario is critical if a collision occurs between the ego vehicle and other vehicles.	Input Sce.: a logical scenario Output Sce.: a set of critical concrete scenarios  Implementation: The method first gives parameter combination of ego vehicle and other vehicles on the road in a scenario, which defines potential paths of them. Exhaustive search algorithm tries to find cases when	Required knowledge: 1. simulation models 2. AD simulator  Validation: This paper applies two case studies, high-way lane change and intersection. Collision scenarios are generated in the case studies.

	prompt a collision between the ego vehicle and other vehicles. The method improves the efficiency in exhaustive search for test cases evaluation.			other vehicles drive in the path of the ego vehicle in a simulator. This is achieved with an iterative manner by firstly including one other vehicle in the scenario and iteratively adding more vehicles (up to 5). Other vehicles try to prevent ego vehicle to reach the goal and collide with the ego vehicle. Through short-distance simulations, uncritical scenarios are excluded and critical scenarios are detected.	
[42]	Activity: Instantiation and criticality check Phase: system verification SOI: control algorithms (ACC and AEB)  This paper proposes a method to search a more critical scenario with a sequential learning approach based on kriging models. The method provides a way to approximate autonomous vehicle behaviors and thus can reduce ontrack experimentation for evaluation.	In the paper, the scenario is limited into lane change situation. A scenario is constituted with three variables, namely 1) the frontal vehicle's velocity, 2) range between the frontal vehicle and the ego vehicle, and 3) time to collision.  Covered layers: 4	In this paper, the criticality of a scenario is estimated by the value of time to collision and distance between vehicles.	Input Sce.: a logical scenario Output Sce.: a set of concrete scenarios with higher levels of criticality  Implementation: The method first utilizes some scenarios as samples and construct an initial kriging model. Then it searches a new scenario point by maximizing the gradient based on the distance of result estimations from the old and new scenario points. It works in an iterative way and the kriging model is updated with new points until the accuracy is satisfied.	Required knowledge:  1. Vehicle dynamic model 2. Initial sampling points 3. A small number of concrete scenario samples as initial observations 4. Simulator 5. A black-box controller 6. SPMD database  Validation: This paper applies the case study in a lane change scenario. The method shows the applicability of searching for the next best scenario with the accuracy of conflict probability evaluation.
[43]	Activity: Instantiation Phase: system validation SOI: control algorithms (ACC and AEB)  This paper proposes an acceleration evaluation method in test case generation. The aim of the study is to provide a more efficient sampling method to discover critical scenarios. The test cases are checked to ensure the	In the paper, the target scenario is the pedestrian-vehicle interaction at a crosswalk. A scenario is described by parameters of pedestrian walking speed, vehicle speed and longitudinal distance. The dataset is built with videos from cameras fixed on the roadside. The videos are processed and crossing events are collected. Parameters are fitted using a truncated Gaussian mixture model (TGMM).	In this paper, a scenario is critical if a crash happens between the ego vehicle and the pedestrian. Risk is classified into different RLSs based on the intensity of actions required to avoid a collision (e.g., required braking acceleration). The safety performance is evaluated with the crash rate in the test.	Input Sce.: raw videos from cameras Output Sce.: a set of critical concrete scenarios under different RLSs  Implementation:  1. Process video files and extract pedestrian-crossing events.  2. Build a pedestrian-crossing model and fit with the TGMM models.  3. Generate initial conditions for testing and classified with different RLSs.	Required knowledge:  1. Videos as raw data and processing tools (i.e., object detection, tracking, calibration, and motion estimation)  2. Model Parametric Toolbox 3 (MPT3) to calculate backward reachable tube (BRT) for initial conditions generations.  3. AD simulator  4. Control algorithms

	feasibility by reachability analysis and assigned with a defined degree of risk by Risk Level Sets (RLSs).			Perform importance sampling in each     RLS to estimate the failure rate.  Examine on the simulator to check the crash rate.	Validation: This paper applies the case study where the ego vehicle is equipped with AEB and ACC. Test samples are generated from both naturalistic distributions and importance sampling distributions. Results from both methods are compared to validate the fast crash rate convergence by the proposed method.
[44]	Activity: Instantiation Phase: system verification SOI: control algorithms (ACC and AEB)  This paper proposes an acceleration evaluation method for autonomous vehicles with importance sampling approach. The results can be used to generate motions of vehicles and further applied in test case generation. The Cross Entropy method is used to guide the choice of importance sampling distribution.	In the paper, the target scenario is the lane change scenario. A lane change statistical model for importance sampling is developed with the data from Safety Pilot Model Deployment (SPMD) database. The scenario is described with initial states of vehicles, including distance between vehicles, ego vehicle's velocity and relative velocity.  Covered layers: 4	In this paper, three kinds of events, conflict, crash and injury, are analyzed respectively in the case study for the evaluation of criticality. A scenario is viewed as critical if the events occur in the simulation.	Input Sce.: a logical scenario including the driver model and the vehicle model Output Sce.: a set of concrete scenarios  Implementation:  1. Identify lane change events from SPMD database and develop a lane change statistical model.  2. Use importance sampling with Cross Entropy method to generate critical scenarios.  Design an autonomous vehicle model and perform simulation to verify the generated scenarios.	Required knowledge:  1. N-FOT data (SPMD database)  2. AD simulator  3. Control algorithms, AEB and ACC  Validation: This paper shows a lane change scenario case study where the ego vehicle is equipped with AEB and ACC. Results show the fast convergence of criticality detection by the proposed method.
[45], [46]	Activity: Refinement of the logical scenario.  Phase: Function verification  SOI: Motion planning algorithm  ODD: structured road  The paper proposes a method to modify a logical scenario. The purpose is to reduce the range of the relevant parameters to the region that contains critical concrete scenarios.	The scenario is defined as the tuple: Initial state of the ego vehicle, trajectories of other traffic participants, and lanes (number and shapes).  A scenario should have a fixed time interval.  All the other vehicles are assumed to stay in the center of its lane with a fixed longitudinal acceleration. Therefore, the longitudinal positions of one trajectory are determined by the vehicle's initial position, initial speed,	A scenario is considered critical if the solution space is small enough.  The solution space is not calculated by the ego vehicle's trajectory planning algorithm, which may consider real-time performance. It is calculated by a generic exhaustive search method. Therefore, the identified scenarios are critical for most of the motion planning algorithms.	Input Sce.: a logical scenario with a specific parametrization. Output Sce.: a "more critical" logical scenario  Implementation: They define the criticality of the scenario based on the solution space that the ego vehicle has.  To find a "more critical" logical scenario, they define an optimization algorithm where the objective is to minimize the solution space of	Required knowledge: 1. Input logical scenarios 2. A way to calculate the solution space (Drivable area). 3. Dataset (NGSIM US 101 dataset)  Validation: They generate "critical" logical scenarios from initially uncritical logical scenarios. But they do not run any simulation to see if their planning algorithms are capable of planning properly.

	and its longitudinal acceleration. The lateral	the ego vehicle (They call it drivable area)	
They do this by calculating the	positions are the center points of the lane.	and the design variables are the ranges (i.e.,	Publication [45] is the newer
solution space of a scenario (They		the upper and lower bounds) of the relevant	version. [46] only allows the
call it drivable area). This solution	The road network is modeled by "lanelets",	parameters (in the case study, they are the	generation of simple scenarios on
space depends on physical	which are atomic, interconnected, and	initial speeds, initial positions and the	straight, non-intersecting roads and
capabilities of the vehicle, and the	drivable road segments. They are defined by	accelerations of the other vehicles. These	only realized translation of other
idea is that the scenario will be	their left and right bound, where each bound	parameters determine the trajectories of	traffic participants.
more critical if the solution space if	is represented by an array of points (a	other vehicles.)	
smaller.	polyline)		
		Then, they use evolutionary algorithms to	
After this process, the motion	Covered layer: 1 and 4	solve this optimization problem. The output	
planning algorithm would be tested		is a logical scenario with smaller parameter	
by running on these scenarios and		ranges.	
having to find a viable solution.			

Table 4. Exploring logical scenarios with parameter trajectories

#	Purpose	Scenario definition	Criticality definition & Surrogate Measure	Solution	Validation & other key observations
[47]	Activity: Instantiation Phase: Function verification SOI: Adaptive cruise control (ACC) Level of Automation: L2 (It only considers the car following scenario with longitudinal control) ODD: car-following within a lane The paper proposes a method to falsify ACC systems by generating motions of the leading vehicle such that the ACC under test causes a rear-end collision.	Covered layer: 4 (only forward movement of one vehicle in front)  They only consider the ego vehicle following another vehicle. The only layer that is covered is layer 4, but only because they define the motion of the vehicle in front. The motion of the ego vehicle and the vehicle in front is in one dimension.  The car-following scenario is modeled	They only consider the car-following scenario.  A scenario is considered critical if it contains motions for the leading vehicle such that the ego vehicle causes a rear-end collision.  Therefore, the proposed method tries to find system-specific critical scenarios.	They use rapidly-exploring random trees (RRT) to generate motions for a leading vehicle such that the ACC under test causes a rear-end collision.  Input Sce.: a logical scenario Output Sce.: a set of critical concrete scenarios  They use two methods to build the RRT:  Forward search: They start with a randomly generated safe state. They calculate the next state based on the ACC control law and the one-	Required knowledge:  - Knowledge about Rapidly-exploring random tress  - Dynamic models of both the ego vehicle and the leading vehicle  - The control algorithm of the ACC (as a black box)  Validation: They used their method to successfully falsify the safety of state-of-the-art ACC systems (They were able to
	They use Rapidly-exploring random trees (RRT) and they propose a forward search and a backward search. They implement the forward search as known in literature, with addition of the definition of unsafe states (When the distance is not enough to avoid an accident in case the leading vehicle performs an emergency brake).	as the motion of the leading vehicle (i.e., its <b>jerk profile</b> ) and the initial state of the ego vehicle (ACC-equipped vehicle).  Each scene contains the positions and speeds of the ego vehicle and the leading vehicle.  The output of the ACC controller is the acceleration of the ego vehicle. The	A critical scenario starts from a safe initial state (or scene) and ends up with a collision state.  A state contains the positions and speeds of both vehicles at a particular time step.  Criticality of a scene: Each scene (i.e., a state) can be classified as:	dimensional vehicle dynamic model. At the same time, they randomly generate the behavior of the leading vehicle (acceleration and jerk). Once they get to an Unsafe state, they make the leading vehicle perform an emergency brake until they get a colliding state.  Backward search: They start at a randomly generated unsafe state, and they try to search backwards in time until they find a safe state. They cannot simulate the ACC vehicle	generate a motion for the leading vehicle such that the ACC under test causes a rear-end collision). They also compared the results to that of existing approaches.
	For the backward search they start in a randomly selected unsafe state and they generate random inputs for the ACC vehicle to try to get the vehicle in the previous state. Then, they simulate forward to ensure getting into an unsafe state again.	behavior (the state ([position, velocity]) at the next time step) of the ego vehicle can be calculated based on the motion of the leading vehicle, the ACC function and a simple one-dimensional vehicle dynamic model.  The motion of the leading vehicle is determined by its initial states and its jerk profile.	<ol> <li>Safe: if the distance between the ego vehicle and the leading vehicle is at least the minimum safety distance to avoid a collision if the leading vehicle performs an emergency brake.</li> <li>Unsafe: If the distance is not enough to avoid an accident if case the leading vehicle performs an emergency brake.</li> <li>Colliding: If the distance between the two vehicles is smaller than 0.</li> </ol>	backwards in time since they cannot compute the inverse of the ACC control law. For this reason, they generate random inputs for the ACC vehicle to obtain the state of the ACC at the previous state. They need to ensure that the ACC system drives the ACC vehicle into unsafe states again.	

		Therefore, a concrete scenario consists of the initial states of both vehicles and			
[48]	Activity: Refinement of a concrete scenario or (Instantiation + criticality check) Phase: system verification SOI: Motion controller  This paper applies functional gradient descent on falsification. It can find a more critical concrete scenario around a given concrete scenario. It can also search within a given logical scenario to find critical concrete scenarios.  The approach is based on multi-fidelity optimization technologies to save computation power. A low-fidelity dynamic model is used when computing the gradient.  Compared to simulated annealing, which takes the system as a black box, the proposed method can provide a better performance in critical scenarios searching.	of the initial states of both vehicles and the jerk profile of the leading vehicle.  Covered layers: Layer 4  A concrete scenario may include Position, velocity (profile), acceleration/deceleration (profile) of the other vehicle and the ego vehicle.  Scene & Scenario: Scene is defined by the state vector at each simulation time. After simulation, a scenario is represented as the trajectories of the states of both dummy vehicle and ego vehicle.  Before simulation, a logical scenario includes the kinematic models and the initial states of both the ego vehicle and the other vehicle(s). A concrete scenario instantiates a logical scenario by fixing the variables e.g., the initial states and the parameters of the kinematic models.  A Scenario should have a fixed duration, which is set 200s in the "stop and go" case study.  The case study evaluates the performance of a Full Range Adaptive	Criticality definition: For the proposed method, the criticality of a scenario is determined by the worst scene criticality. The criticality of a scene is defined by relevant KPIs.  The proposed method can find Critical scenarios for a particular system.  In the case study, Maximum absolute jerk (MAJ) is used to evaluate the comfort performance of the motion controller. Jerk is calculated for each scene, among which, the worst one is chosen as the MAJ.	Input: Concrete scenario Output: Critical concrete scenario  Implementation: The method applies functional gradient descent to search critical scenarios. The objective function contains the relevant KPIs, which are calculated based on the initial states and the kinematic models.  KPIs are calculated for each scene. When calculating the gradient at each iteration, the critical scene (i.e., the scene with the worst KPI) needs to be found first. The gradient is calculated on the critical scene with low-fidelity kinematic models.  According to our understanding, the approach assumes that the critical time will converge during the gradient decent. In other words, when refining a concrete scenario, it normally finds a more critical scenario with similar critical time.	Required knowledge:  A low-fidelity model for the implementation of functional gradient descent calculation.  A high-fidelity model for the evaluation of system performance with certain input parameters.  The algorithm to calculate functional gradient descent and update input signal.  A given logical scenario for searching or a given concrete scenario for refinement.  The control algorithm of the motion controller.  Validation: The case study demonstrated in the paper proves the effectiveness of the method. In the case study, the results generated from functional gradient descent approach outperform that from simulated annealing in terms of worst-case performance value. Experiments generated from gradient descent has better average performance improvement than simulated annealing.
		Cruise Control (FRACC) controller using maximum absolute jerk as a critical metrics. The variable of this logical scenario is the acceleration profile of the other vehicle. All the other parameters are fixed.			

			T	T	
		To save computation power, a low-			
		fidelity dynamic model is also needed.			
[49]	Activity: Instantiation	Covered layer: 1, 2 and 4 (They also	A critical scenario refers to the one	Input: A logical scenario	Required knowledge:
	Phase: Function verification	mention 5 but they do not show it in	where the ego vehicle has to break	Output: concrete critical scenarios	A logical scenario (agents of interest)
	SOI: control policy	the examples)	its rule due to the legal behaviors of		Rulebooks
			other agents.	Deep Q-learning (a reinforcement learning	The dynamic model (the relating
	They propose an adversarial testing	The variables can cover layer 2, 4 and 5		method) is used to learn the behaviors of the	between the states and actions) of each
	methodology in which they train			adversarial agents. At each time step, it updates	agent
	adversarial agents to demonstrate	1-Street: The simulations show	The rules for the adversarial agents	a q-function (a look-up table). Its inputs are the	A simulator (CARLA)
	flaws in the behavior of the ego agent.	scenarios in CARLA, but the definition	are prioritized. Some of the rules of	current states of the agent, the observed states	, ,
		of the environment is not included in	the adversarial agents are allowed to	of the other agents and one action that the	Validation: The proposed method has
	The purpose of the adversarial agents	the scenario.	be broken when searching for action	agent will take. Its output is the quality of that	been verified in three case studies:
	is to force the ego vehicle to break its	<b>2-Traffic infrastructure</b> : One of the	profiles. If necessary, rules with the	action. The q-function is trained based on all the	following an adversarial agent on a
	rules. The adversarial agents are	examples involves a traffic light	lowest priorities will be broken first.	previous data and the objective function	single-lane freeway, driving on the
	constrained to follow the traffic rules.	changing the state.		mentioned before. If the action improves the	freeway when an adversarial agent
	The rules for both the ego vehicle and	<b>4-Movable objects:</b> Some of the states	During the searching, the objective	objective function, the quality value of that	performs a cut-in maneuver, coming to
	the adversarial agents are described by	of other vehicles around the ego	function (to be maximized) is a	action under those states will be increased.	an intersection with a yellow light behind
	Signal Temporal Logic.	vehicle is known (some states are	weighted sum of a set of Boolean		an adversary.
		hidden)	variables, each of which refers to the	During simulation, the actions with the highest	
	As pointed out in the paper, the	5-Environment conditions: They	satisfaction of a rule. The ones for	quality value will be chosen.	Question: The objective function is
	proposed method can also be used to	mention that weather patterns can be	the rules of the ego vehicle should	Their method consists of training adversarial	calculated based on all the previous
	falsify the whole system, since the	modeled as being controlled by agents,	have negative weights. The others	agents to challenge the ego vehicle (i.e., to force	states, which are determined by all the
	environmental conditions (e.g.,	but that it not shown in the examples.	should have positive weights. The	the ego vehicle to break its rules).	previous actions. Why does the update
	weather) can also be modeled as an		absolute values of the weights		process only update the quality of the
	agent with changing states.	A scenario consists of a collection of	represent the priorities of the rules.	Each simulation has a fixed duration. The q-	current action? I think it should update
		agents together with rulebooks that		function is trained by many simulations	the quality values of all the previous
		specify constraints on their behaviors		(episode). For each simulation, the initial states	actions.
		(together with the rulebook for the ego		are randomly selected.	
		vehicle). Everything in the scenario			
		with changing states can be modeled			
		as an agent. Therefore, no			
		environmental model is needed.			
		The variables of a logical scenario are			
		the potential states of the agent and			
		actions that the agents can make at			
		each time step, i.e., <b>the state and</b>			
		action profiles of all the agents of			
		interest (other than the ego vehicle).			
		miterest (other than the ego vehicle).	1		

- [50] **Activity:** Refinement of concrete
- [51] scenarios and simulation
- [52] **Phase:** System Validation
- [53] **SOI:** Planning and control

Adaptive Stress Testing (AST), which was first applied in the literature to test an aircraft collision avoidance system, formulates the scenario space as a Markov decision process (MDP). The original method uses Monte Carlo tree search (MCTS) to search for the most likely failure condition.

The contribution in [50] is:

- To extend the AST methodology to use Deep Reinforcement Learning (DRL) as the solver technique.
- To apply AST to a set of autonomous vehicle scenarios.

The contribution of [51] and [52] is to improve the reward function. They propose:

- A different reward function for the ATS using RSS to find scenarios where the ego vehicle performs unproper actions.
- A trajectory dissimilarity reward to promote the discovery of highly diverse failure scenarios.

In [53], the authors extend the work developed in [50] by replacing the original Multi-layer perceptron (MLP) network with a Recurrent neural network (RNN).

**Covered layer:** 1, 4 and performance limitation of the ego vehicle (i.e., the sensor noise).

The variables of the logical scenario only cover layer 4 and the noises on the detected speeds and positions of other agents.

A scenario is described by the (perceived) state profiles of all the relevant agents (ground truth states + noises).

In their case study, there is a road with a crosswalk and a pedestrian walking on the crosswalk as the agent.

**Layer 1:** The road is contained in the model, and they also model a crosswalk

**Layer 4:** The pedestrian is a movable object

**Performance limitation:** the noises

In [50], a scenario is considered critical if a collision occurs, regardless of how the collision occurs. For this reason, in some of the results obtained, the pedestrian is considered responsible after analyzing the scenario.

The algorithm is penalized for not finding a collision. This penalty also depends on the distance between the car and the pedestrian.

In [51], a scenario is considered critical if it reaches a set of predefined critical states e.g., getting too close to another agent or colliding with it.

In this work, the proposed method tries to find such critical scenarios with as many improper actions of the ego vehicle as possible.

The improper actions are defined according to RSS.

In [53], a scenario is considered critical if a collision occurs. In this study, all the transitions are deterministic with respect to the system under test (SUT). For this reason, the scenario is defined by the starting conditions and the sequence of actions taken by the SUT.

Input: A non-critical scenario
Output: A critical scenario

They use a variation of Adaptive Stress Testing (AST).

AST formulates the scenario space as a Markov decision process (MDP) and is usually solved using a Monte Carlo Tree Search (MCTS) or a Trust Region Policy Optimization (TRPO).

In [50], they propose to use a Multi-layer perceptron (MLP) as solver to find the failures. They compare the results obtained against a Monte Carlo Tree Search (MCTS) and Trust Region Policy Optimization (TRPO) because both have been shown to successfully find failures when combined with AST, showing that they can find failures more efficiently.

The main contribution of [51] is on the improved reward function, which contains three parts:

- (1) The identified solutions should divers as much as possible.
- (2) The identified solutions should force the ego vehicle to make improper actions as many as possible.
- (3) The sampled actions of the agents at each time step should not diverge too much from their expectations.

In [53], the authors propose two implementations:

 Discrete recurrent deep reinforcement learning (DRDRL): The RNN implementation only requires the previous state of the network. This solver can only be run from a single initial condition.

## Required knowledge:

- RSS (Only in [51])
- Simulator

## Validation:

In [50], they apply AST with DRL on a scenario involving an autonomous vehicle and pedestrians and show that they are able to find scenarios that lead to a collision.

In [51], they apply AST with an augmented reward on a scenario involving an autonomous vehicle and pedestrians and show that they are able to find more improper response when compared with an existing AST setup.

In [53], they apply AST with DRL on a scenario involving an autonomous vehicle and pedestrians and show that they are able to find scenarios that lead to a collision. Also, they compare the results between the two architectures proposed, showing that the generalized architecture (GRDRL) outperforms the discrete architecture (DRDRL)

	The reason for this is that the previous implementation required the current state of the simulation as input for the network, which imposes many limitations for the implementation with real complex simulators.  To solve this, the authors propose to define the scenario by the starting conditions and make all the transitions deterministic with respect to the system under test (SUT). This way, the solver does not need to get the state of the simulation at every step, allowing the simulation to be considered as a black box.			- Generalized recurrent deep reinforcement learning (GRDRL): The RNN implementation requires the initial state of the simulation as an input and the previous state of the network. The hypothesis is that by accepting the initial state as an input, the network can learn a policy that generalizes to the entire space of initial conditions. During the training, each rollout starts from a randomly sampled initial condition.	
[54]	Activity: Instantiation Phase: System verification SOI: Planning and control  The purpose of the study is to generate test cases in the boundary where the autonomous vehicle can no longer avoid a collision (almost-avoidable collisions or near-misses).  They propose their custom version of RRT with a custom cost function. This cost function promotes collisions that are almost avoidable.	Covered layer: 4  The street layer is represented when sampling target path segments. The example used is for a straight road, but the authors mention that a coordinate transformation can be applied for sampling from curved roads.  Perception result is derived from a simulator and is assumed to be deterministic.  The movement of the other movable objects is decided by the RRT algorithm to find the most critical scenarios.  It searches for the initial condition and the control outputs of the other vehicles at each time step.	In this study, they are only interested in scenarios in the boundary where a collision is almost avoidable.  They do not take into account what actor is responsible for the collision, only if a collision occurs.	Input: A logical scenario Output: A critical scenario  The purpose of the study is to generate test cases in the boundary where the autonomous vehicle can no longer avoid a collision (almostavoidable collisions or near-misses).  They propose their version of RRT with a custom cost function. This cost function promotes collisions that are almost avoidable.  - A collision between an Ego vehicle and an agent that could have been avoided with a minor change in the control applied or agent trajectories  - An almost-collision (near-collision) which could have resulted in a collision with a minor change in the control applied or agent trajectories.  They estimate how avoidable was the collision by using:  - Ratio of the collision surface  - Collision speed  - Minimum time to collision	Required knowledge:  - Knowledge about the simulator  - Knowledge about the kinematic models  Validation: They have applied their method to a case study with 4 agents and one ego vehicle, being able to find scenarios that lead to a collision.

	T	T	T		
[55]	Activity: Refinement of concrete scenarios Phase: System verification SOI: Decision and Control parts of ACC	Covered layer: 4  In this paper, a scenario is defined by the trajectory of the control input of	In this study, a scenario is considered critical if it leads the system to violate the requirements. Each requirement is modeled on a critical scene. For	Each node in the tree includes the state of the system and the simulation time. When the tree grows, instead of running the simulation from the initial state, only a partial simulation is executed from an existing node of the tree to the new node.  Input: A concrete scenario Output: A critical concrete scenario The process to search for critical scenarios is	Required knowledge:  - The order of the system model  - real test or simulation or some kinds of driving data to measure the state
	(in the case study)  The purpose of the study is to generate	the SOI.  In the case study, there are three	example, the distance between the leading vehicle and the first following vehicle should not be less than 5m.	formulated as an optimal control problem, which finds the optimal sequence of control input (in the case study, it is the acceleration	response (in the case study, they use a simplified dynamics model called "Optimal Velocity car-following
	input trajectories (sequences of inputs) to falsify the requirements of a system.  They use ACC as an example. The	vehicles platooning in the same lane. The SOI is a longitudinal ACC controller, which controls two vehicles following a leading vehicle. The scenario is then	The violation of this requirement is modeled as the advent of the first scene where the distance exceeds 5m.	profile of the leading vehicle and the time instances of critical scenes) to optimize the objective function.	Model")  Validation: They have applied their method to generate a scenario that
	trajectory is a sequence (over time) of inputs. In the use case it is the acceleration profile of the leading vehicle. The same ACC algorithm is used to control two flowing vehicles.	defined as the trajectory of the longitudinal acceleration values of the leading vehicle (i.e., the design variables) and the dynamics of the two following vehicles.	A strong assumption made by this paper is that the order of the advents of the critical scenes are known. It is possible that some critical scenes do not appear. But if they occur, they	The system (including the states of the three vehicles and the ACC controller for the two following vehicles) is formulated as nonlinear differential equations. The proposed method assumes that the model of the system is not known except the order of the model.	falsifies an ACC system. The identified critical trajectory is not validated.
		Parameters for criticality evaluation include the distances between vehicles and the speeds of the two following vehicles.	should follow the pre-defined order.  The objective function of the searching process includes two parts. The first part maximizes the number of critical scenes. The second part minimizes the total length of the scenario.	The optimization iteratively refines the given trajectory (as an initial nominal trajectory). In each iteration it:  1. identifies the system (as a linear system) around the nominal trajectory with local time-varying model identification method by exciting the system n times (n = the order of the system) to get n independent state	
				responses.  2. gradient-based method is used to update the parameters (the trajectory and the time instance).  3. Uses the new parameters to generate a new nominal trajectory.	

[56]	Activity: Instantiation	Covered layer: 1, 4	In this paper, a scenario is critical if it	Input: A logical scenario	Required knowledge:
,	Phase: V&V SOI: Motion Control algorithms	From the use cases	violates a given safety specification, criticality is defined based on	Output: A critical concrete scenario	- System dynamics model (assumed to be linear)
	This paper proposes a method to find avoidable critical scenarios with controller synthesis method. Criticality is defined based on a set of predefined specifications. Avoidability is derived with controlled invariant set.	A falsifying scenario consists of two parts: an initial condition and a disturbance input profile.  In the (ACC + Lane keeping) case study, the initial condition (also the system states) includes:  • The longitudinal velocity of the ego vehicle,  • The longitudinal velocity of the lead vehicle,  • The distance between the two vehicles,  • The lateral deviation from the lane center,	specifications, together with a certificate that it is possible to satisfy the specification for this initial condition and disturbance, as long as the control inputs are within their range.  Specifications are formally defined with first order logic. In the case study the specifications are:  • the control input should stay within specified bounds.  • whenever the lead car is closer than a certain value, the time headway needs to be greater than	The first step is to divide the system states into three sets according to system dynamics model:  1. Controlled invariant set: It is a subset of safe states. For states in this set, as long as the disturbance is within its range, it is always possible to find a control input so that the next step state is also in this set.  2. Dual game winning set: It is a subset of safe states. It is also the complementary set of the controlled invariant set.  3. Unsafe states: States that violate the specifications.  Step two is to sample the states (on the boundary or interior area) in the controlled	- Controller algorithm (black box) - Safety specifications  Validation: They have demonstrated their approach in two autonomous driving functions, adaptive cruise control and lane keeping. The applicability of this method is validated on two simple controllers and a realistic one provided by Comma AI. The efficiency of the method is validated by comparing the result with S-TaLiRo.
		<ul> <li>The lateral velocity,</li> <li>The yaw-angle deviation, and</li> <li>The yaw rate.</li> </ul> The disturbance includes the longitudinal acceleration of the lead car, and the road curvature.	a threshold.  Lateral deviation, lateral velocity, yaw angle deviation and yaw rate should be within certain thresholds.  The control inputs are:  the net force acting on the mass of the following car (the ego vehicle).  the steering angle of the front wheels.  Note: In the case study, there is no specification for lateral control.	invariant set to obtain potentially interesting initial conditions.  Step three is to calculate the strategy of disturbance to lead the system moving from dual game winning set to unsafe states. In this step, the controller is not necessary.  Step four is to calculate the strategy of disturbance to lead the system moving from a state in the controlled invariant set to dual game winning set. In this step, the controller is needed as a black box.	
[57]	Activity: Instantiation Phase: System verification SOI: Planning and control	Covered layer: 4  Layer 1 is represented by a map of the area discretized with a resolution of 1.5	A valid test scenario is the one that requires the AV to avoid a collision with a pedestrian, given that the pedestrian intercepts the AV path in	Input: A logical scenario Output: A critical concrete scenario At the beginning, the agents (pedestrians) are	Required knowledge: - Assumed behavior model of the pedestrians.
		area alsoretized with a resolution of 1.5	pedestrian intercepts the //v path in	randomly placed using the spawn locations. At	

This paper proposes the generation of	meters. (not represented in the	a way that the collision can be	each simulation tick the agents behave	Validation: The have developed a case
test cases using agency-directed test	scenario space.)	avoided.	depending on their class (random or directed).	study where the emergency stopping of
generation.			The possible actions are standing still, moving	an AV is tested by pedestrians getting
	Layer 4 is represented by the	Scenarios are also scored to	forward, backward, left or right.	into the road.
They propose to use a multi-agent	pedestrians. They can have a random	encourage more realistic scenarios. A	The test finishes when the assertion (forcing the	
system (a system where multiple	behavior or an agency-directed	living cost is assigned to promote	AV to stop) is reached or when the AV gets to	
intelligent agents interact in order to	behavior where the agent's perception	shorter tests and a penalty is also	the end of the road.	
solve a problem) to generate test cases	is taken into account.	given depending on how long the		
that would force the autonomous		pedestrian spends on the road.		
vehicle to react to avoid a collision.				

Table 5. Finding critical scenes for CV-based functions

#	Purpose	Scenario definition	Criticality definition& Surrogate Measure	Solution	Validation & other key observations
[58] Scen ic	Activity: Logical scene modeling & Instantiation & improvisation & assessment & influential factor analysis  Phase: component design  SOI: CV function  The proposed method can generate scenes (pictures) according to a given scenario description.  It supports the training and testing of machine learning models. E.g.,  1. Generating Specialized Test Sets (e.g. partial occlusion, bad weather, or bad illumination)  2. Retraining to Improve Performance on Hard Cases (i.e., adding specific types of images (e.g., images with occluded vehicles) to the training set)  3. Generalizing from a Known Failure Case (e.g., to identify the most influential features to certain misclassifications and use that to guide the retraining)  It can be used in the function development phase	Scene: a set of configurations of objects in space. Generated scene: a picture  According to our terminology, a scenario in this paper should be called a logical scene.  A Domain-specific language is proposed to model a scenario (i.e., a logical scene). It covers: Scenario Configuration:  Configurations of Objects Relations between objects Time Weather  Object configuration Position Heading Road deviation: the heading of the car with respect to the local direction of the road Size Car model (including color) View range: to define the 'can see' predicate  Relations between objects Relative position Can see (if A can see B, B is in the view range of A.)  Not all these factors need to be specified in the scenario description. The user only needs to specify the ones of interest.	The purpose of the tool is to test the CV function under known critical scenes and to find the influential factors.  Critical scenes are defined as the scenes that may cause the unintended behaviors of the camera perception functionality. E.g., miss detection, clutter detection, miss classification, etc.  The proposed method can generate both generic and system-specific critical scenes.	Input: logical scene described in the proposed language Output: A set of scenes satisfying the given description  Scene improvisation: Given a (partially) defined scenario, the improviser generates a set of scenes (pictures) that satisfy the scenario definition (i.e., the logical scene). The improviser uses a rejection sampling approach.  Objects will be placed in a game engine (GTA V) according to the scenario description and physical constraints (e.g., cars are on the road, cars do not overlap, etc). Unspecified factors (e.g., the background, road structure, car model) will be randomly selected. For the background of the generated scene, the tool will put all the objects at a random place in the city in the game.  A snapshot from the ego vehicle's perspective is taken as one generated scene.	Required knowledge: 1) Env. Model (appearance) (given by GTA V) 2) Implementation of the CV functions. 3) Interesting logical scene (either identified potentially risky scenarios or a complete set of scenarios)  Validation: Targeted data augmentation improves functional performance. Augmented data was designed according to an analysis of the influential factors.

		Covered layers: Scenario config. 4,5			
		Generated scenes: 1,4,5			
		Since it only generates scenes, therefore, content in layer 4 (e.g., vehicles and pedestrians) are static.			
[59]	Activity: Scene refinement	Definition of scenario is not explicitly given in the	In this paper, 'critical	Input scene: scene with good weather	Required knowledge:
Dee	Phase: component design /	paper.	scenario/scene identification' is	Output scene: scene with bad weather	1) real-world driving scenes
pRo ad	verification SOI: CV function	This paper explored and synthesized various	not mentioned.	Scene generation: Based on the	2) Videos with extreme weather
au	SOI: CV function	driving scenes including those with rather extreme	In this paper, scenes with bad	Generative Adversarial Networks (GANs)	conditions
	DeepRoad, an unsupervised	conditions.	weather are considered as critical.	technique, images with the two extreme	Validation:
	framework	In particular, images with two extreme weather	Wedner are considered as critical.	weather conditions were collected from	A case study to show how added bad
	o to automatically generate large	conditions, including heavy snow and hard	They assume that scenes with bad	Youtube videos to transform real-world	weather conditions will affect the driving
	amounts of accurate driving	rain, were collected and synthesized.	weather may cause unintended	driving scenes and deliver them with the	behaviors of E2E learning AD functions.
	scenes with various weather		behavior of the CV functions.	corresponding weather conditions.	
	conditions (including those with	As we understand, this paper was not aimed for			Here the driving behavior refers to
	rather extreme conditions).	identifying critical scenarios, but rather for testing		Testing: Metamorphic testing.	steering angle, which is the output of
	<ul> <li>to test the consistency of three well recognized DNN-based</li> </ul>	autonomous driving functions with synthesized scene. From this perspective, driving scenes under		Metamorphic relations are defined such that regardless of how the driving scenes	different DNN-based autonomous driving models. It is claimed that 'Since the road
	autonomous driving systems	extreme weather conditions, including heavy snow		are synthesized to cope with weather	scenes should not largely impact the
	across different scenes.	and hard rain, were initially regarded as critical		conditions, the driving behaviors are	steering angles, any inconsistency may
	deross different seeffes.	scenes.		expected to be consistent with those	indicate correctness or robustness issues
	It can be used in the system testing			under the corresponding original driving	of the systems under test.'
	and verification phase.	Covered Layers: It adds information on layer 5 to		scenes.	Key assumption: the road scenes should
	·	an existing scene, which contains layers1, 2, 4, ,5.			not largely impact the steering angles.
				Metric: the number of inconsistent	
				behaviors of autonomous driving	
[00]				Systems.	
[60]	Activity: Assessment	Definition of scenario is not explicitly given in the	The critical scenario is not	Input Scene: Scene before the	Required Knowledge:
Dee pTes	Phase: component design /	paper.	mentioned in this paper.	implementation of image transformations.	Real-world driving condition scene.
t pres	verification	This paper generates synthesized scenes by	However, we can assume that the	transformations.	Validation Metrics:
`	vermouton	applying different image transformations.	scene with bad weather conditions	Output Scene: A new scene resulted	The correlation between input-output
	SOI: end-to-end learning		or by changing the lightning	from implementing image	diversity and neuron coverage.
			conditions can affect the	transformations process.	
	DeepTest is proposed for	This paper is aimed for testing the DNN capabilities	capabilities of DNN, thus, may lead		In this metric, they tried to make sure
	automatically detecting erroneous	for autonomous vehicle instead of identifying	to critical scenario.	Scene generation: By implementing nine	whether neuron coverage is a good
	behaviors of DNN-driven (end to end	critical scenarios. From this perspective, driving		different realistic image transformations	

learning) vehicles that can potentially lead to fatal crashes. Also, it proposed to increase the neuron coverage of DNN models such that the accuracy of DNN models can be increased.

- Leverage the notion of neuron coverage to explore different parts of DNN logic.
- Applied different image transformations that mimic realworld conditions (e.g., changing contrast, adding rain) in driving condition to maximize the neuron coverage of DNN.
- They also generated a new image by using greedy algorithm in order to increase the neuron coverage.
- Automatically detect the erroneous behavior with neuron coverage guided the synthesized images.

scenes under extreme weather conditions and lightning conditions can be regarded as critical scenes.

**Covered Layers:** It adds information on layer 5 (by doing image transformations) to an existing scene, which contains layer 1, 2, 4, 5.

In particular, for blurring and adding fog/rain effects, they used convolutional transformation.

They used four different types of blurring filters (e.g., averaging, Gaussian, median, and bilateral) for the blurring. And Adobe photoshop was used for composing these multiple filters.

## Methodology:

Systematic testing with neuron coverage.

They mentioned the formula how to calculate neuron coverage. And based on the formula, will be used to guide their greedy optimization algorithm.

They calculated neuron coverage by dividing the ratio of unique neurons get activated for given input and the total number of neurons in DNN.

Increasing coverage with synthetic images.

Implement image transformations to the scene to show how the results of image transformations can affect driving behaviors (e.g., steering angle and steering directions) of DNN-based AV.

Moreover, it is also intended to show how the neuron coverage of DNN, the number of activated neurons, and the accuracy of DNN are affected because of the image transformations.

 Combining transformations to increase coverage. metric to capture the functional diversity of DNNs.

For instance, the neuron coverage changes with the changes in output steering angles, i.e., different neurons get activated for different output.

And based on the results showed above, the neuron coverage is correlated with input-output diversity of DNNs.

- The set number of activated different neurons affected by image transformations.
- The extent of neuron coverage affected by the combination of image transformations.
- The number of erroneous behaviors of DNN models that can be detected by DeepTest.

The accuracy of DNN models.

				6: 1: 1: 1:	
				Since each individual image	
				transformation increased neuron	
				coverage, they also tried to find	
				whether combined image	
				transformations can increase the	
				coverage by using this method.	
				In this method, they used greedy	
				algorithm to find efficiently the	
				combination of image transformations	
				that result in higher coverage.	
				Find critical scenarios:	
				They find the critical scenario based on	
				the erroneous behaviors detected by	
				DeepTest using synthetic images.	
[61]	Activity: Criticality assessment	Definition of scenario is not explicitly given in the	This paper defines critical	Input Scene: Original images from the	Required knowledge:
	,	paper.	scenarios as corner cases.	datasets.	Image datasets
	Phase: component design /				DNN algorithms
	verification	Covered layers: 5 and noises on camera.	Corner case definition: the	Output Scene: Transformed image by	
		•	unexpected behavior from the cars	DeepXplore.	Validation:
	SOI: end-to-end learning	This paper adds additional information on layer 5	which may leads to critical		The evaluation is based on the numbers
	<b>0</b>	such as intensifying the light condition and adding	scenario.	Datasets: They used five datasets in	of erroneous behaviors found by
	This paper proposes a tool named	tiny black rectangles for simulating effects of dirt		which three of datasets contain images	DeepXplore and numbers of neuron
	DeepXplore to test and validate the	on camera lens by implementing image	<b>Example</b> : a scene with different	(hand-written digits, general images, and	coverage.
	performance of Deep Learning	transformations.	contrast or brightness could lead	driving video frames). And the other two	0010.080.
	systems. It is the first testing tool to		to corner case. This corner case	datasets contain PDFs and android apps.	Limitations:
	measure the performance of DNN		should be detected by the DNN as	Only the driving video frame database is	It only considers a small set of image
	according to the authors claim.		erroneous behavior to achieve	related to our survey.	transformations; thus, it does not fully
	C		reliable systems.	,	capture all real-worlds conditions.
	In this paper, they are not		<i>'</i>	Joint Optimization Problem:	The gradient information-only is not
	particularly building the tool for		In this paper, they used	DeepXplore formulated the joint	fully be able to compute many
	DNN-based system for self-driving		transformed scene to generate a	optimization problem to generate new	realistic transformations accurately.
	cars. However, they evaluate		corner case.	test input that can maximize the neuron	The proposed method cannot
	DeepXplore with one of datasets that			coverage and exposing many differential	guarantee the absence of errors.
	contain driving video frame to			behaviors (i.e., differences between	guarantee the absence of en ors.
	evaluate DNN for self-driving cars.			multiple similar DL systems). And, after	
				the optimal result is obtained, then it will	
	DeepXplore is the extended version			implement specific-domain constraints to	
	of DeepTest.			achieve a realistic and valid input tests.	
	or bechiest.		<u> </u>	acineve a realistic and valid input tests.	

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				It has two objective functions:  1. Maximizing differential behaviors.	
				The first objective of the optimization	
				problem is to generate test inputs that	
				can induce different behaviors in the	
				tested DNNs, that is, different DNNs will	
				classify the same input into different classes.	
				Classes.	
				2. Maximizing neuron coverage.	
				To achieve a maximized branch	
				coverage of the testing	
				Cases.	
				Specific-domain constraints: this paper	
				have two major types of constraints	
				which are:	
				Image constraints.     Other constraints.	
				Other constraints.  The image constraints are used for image.	
				transformations to the image datasets.	
				Image transformations: They	
				implemented image transformations	
				based on the specific-domain constraints to generate new test input images. The	
				image transformations that they used	
				include adding lighting effects, occlusion	
				by single rectangle, and occlusion by	
[0.7]				multiple rectangles).	
[62]	Activity: Criticality (complexity)	Definition of scenario is not explicitly given in the	In this paper, criticality is	The propose Graded Offline Evaluation	Required knowledge:
	assessment  Phase: offline testing and validation	paper.	considered as scenario complexity.	<ul><li>(GOE) framework includes:</li><li>multi-sensor data grading (in terms of</li></ul>	<ol> <li>Ungraded scenario data</li> <li>Ontology of the scenario</li> </ol>
	<b>SOI:</b> Perception tasks	<b>Covered layers:</b> 1,(2), 4, 5	Scenario complexity is not formally	complexity) with the semantic	configuration (i.e. the sematic
			defined. It is classified into three	descriptor	descriptor).
	They assume that driving conditions	Scenario Configuration:	levels as Simple, Medium and	cognition task list	
	with different complexity have	• road type (layer 1)			

	different requirements to the cognitive ability (i.e., complex driving condition requires high cognitive ability) to guarantee safety.  Therefore, they propose a framework to determine the driving complexity (graded into three levels) of the scenes in naturalistic driving datasets so as to evaluate if the cognitive tasks (SOI) fulfills the required cognitive abilities for different driving complexities.	scenario content (layer 1)     challenging conditions (layers 4 & 5)  scenes from classical naturalistic driving datasets are manually encoded into semantic descriptors (i.e., a vector).  There is no clear definition of each scenario configuration, but a list of example factors is provided.	Complex, according to scenario configuration values.  Complexity of each semantic descriptor is judged by expert experience.	Cascaded Tanks Model based offline evaluation and results analysis     Visualization  Criticality (complexity) checking: Input sce.: executable scene (image or sensor input at one time instance) Output: The complexity of the scene  Sensory data (image or sensor data) is manually encoded into a proposed Semantic Descriptor, which is further classified into 3 levels of scenario complexity by an SVM classifier. The SVM was trained according to expert knowledge.  Function evaluation on scenarios with different complexity:     With the graded and annotated offline testing data and the predefined cognition tasks, the cognition abilities are evaluated with the Cascaded Tanks Model.  The Cascaded Tanks Model provides the cognition performance of the AV at different scenario complexity.	3) Expert knowledge to grade Scenario complexity for the training of the SVM.  Inputs for the cognition validation: 1) threshold indicators of fail/pass of cognitive algorithm /modules 2) weights of different cognition task  Validation: A case study to show the proposed framework can evaluate cognition tasks under different complexity. But they did not validate the classified complexity of each scenario.
[63]	Activity: Criticality (Complexity) Assessment	Definition of scenario is not explicitly given in the paper.	In this paper, criticality is considered as scenario complexity.	The scenario complexity is computed from two perceptual data levels:	Required Knowledge:  • Ungraded scene data
	Phase: Offline testing and validation			Road semantic complexity (RSC) → It	Ontology of the scenario
	SOI: Perception Task	Covered layers: 1, 2, 4, 5	Scenario complexity is not formally defined. It is classified into three	is based on support vector regression in which it predicts by learning the	configuration (i.e. the sematic descriptor).
	Motivation: it often requires massive	This paper uses semantic descriptor to classify the scene. Specifically, the classification is considered	levels as Simple, Medium and Complex, according to scenario	relationship between the road label and semantic descriptor.	Validation.
	amount of traffic scenario datasets to	from two levels:	configuration values.	<ul> <li>Traffic element complexity (TEC) → to</li> </ul>	Validation: Implement the proposed method in their
	perform an off-line testing and	nom two levels.	comparation values.	measure the complexity with the	off-line test task to speed up the process.
	performance evaluation of UGV.	Through vector to describe the semantic	Furthermore, scenario complexity	respect to the moving traffic entities	on-line test task to speed up the process.
		characteristics of road scene.	is measured on the basis of road	such as nearby vehicles.	In specific, the off-line test data are
	These traffic scenario datasets		types, scene types, challenging		having 2000km. The data are derived
	provide data support which include		condition and traffic elements.		

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	various annotations (e.g., types of	Specifically, for describing the road scene, they	The final calculation of any	Input: Scene data in datasets.	from the scene video data and the 3D
	scene and roadways).	defined the semantic descriptor from three	The final calculation of scenario		laser point cloud collected by the real
		levels: road types, scene types, and	complexity is obtained by the sum	Output: The complexity of scene.	road.
	However, the existing database lacks	challenging conditions. And a vector is used to	of quantified road semantic		
	the quantitative description of scene	each level to represent the complexity value.	complexity and the traffic element	Complexity checking for RSC:	
	data complexity and scene	The vector value is 0 or 1 for road types and	complexity.	Scene data are encoded to semantic	
	characteristics.	scene types. And the vector value for		descriptor. In particular, the semantic	
		challenging conditions is 0, 0.2, 0.4, 0.6, 0.8, 1.		descriptor is defined from three levels:	
	Thus, this paper proposes a method	<ul> <li>Through matrix to describe the topology</li> </ul>		Road types	
	in quantifying scenario complexity to	information of traffic elements.		Scene types	
	rank massive scene data.			Challenging conditions	
		Particularly, they used Nx2 matrix where the			
	Moreover, they claimed that there is	first column is appointed for the value of		In here, SVR is used to automate the	
	usually a negative correlation	distance from car to car. The second column is		scene complexity task by exploiting the	
	between the unmanned vehicle	assigned for the value of car's viewpoint which		relationship between the road marking	
	algorithm and scenario complexity.	obtained from 8-nearest neighbor of		complexity and the semantic descriptor.	
	, ,	viewpoint from ego vehicle.		complexity and the semantic descriptor.	
	Hence, the complexity of the scene			Complexity checking for Traffic Elements	
	data needs to be incorporated for			The scene is encoded to the matrix of	
	reliable evaluation of UGV systems.			traffic elements. The traffic elements are	
	, , , , , , , , , , , , , , , , , , , ,			reflected by semantic data in two	
				aspects: distance and angle.	
				aspects. distance and angle.	
				Each row in the matrix of traffic element	
				represents each car's information.	
				1. First column: for the distance from car	
				to car.	
				2. Second column: for the car's	
				viewpoint.	
				The matrix is obtained from the	
				calculation of point cloud collected by	
				LIDAR. And based on the matrix, the	
				complexity of traffic elements can be	
				calculated.	
]	Activity: Criticality check of concrete	In this work, no clear definitions are given to	According to our understanding,	Input Sce.: A video stream	Required knowledge:
t	scenarios (video streams)	scenario and scene. Instead, they use the term	critical scenarios in this paper are	Output: Criticality	an image prediction algorithm
)	Phase:	"corner case".	interoperated as corner cases.	- Supplier Criticality	- an image prediction digorithm
'	i nase.	COLLICI CASE .	interoperated as corner cases.	process:	
				hioress.	

	operation phase: Online corner	The word 'case' is not defined. Corner case is	Corner case definition: non-	According to the previous frames in a	a a computie cogmontation algorithms to
	case detection	clearly defined.	predictable relevant object/class in	video stream, the next frame will be	• a semantic segmentation algorithm to identify relevant objects
	developing phase: offline corner	Corner case definition: non-predictable relevant	relevant location.	predicted by a given image prediction	
		object/class in relevant location.	Televant location.	algorithm.	Cityscapes dataset     Datastics System to calculate assume
	case detection (for training	object/class in relevant location.	If a critical frame is detected, the	The predicted image is compared with	Detection System to calculate corner
	algorithms)	So, according to our understanding, a scenario (or	video stream containing this frame	the actual frame in the video stream.	case score
	<b>SOI:</b> perception system	a case) mainly refers to a video stream.	and its previous frames is		• threshold value of corner case score.
	This paper proceeds a mothed to	a case, mainly refers to a video stream.	considered as a corner case.	A semantic segmentation algorithm is used to detect if there is a relevant	Howards aster
	This paper presents a method to detect corner cases in video streams.	Covered layers:	considered as a corner case.	object in the frame. If there is no	Hypothesis:
	detect corner cases in video streams.	The main concern is on layer 4	A frame in a video stream is critical	1 -	As a working hypothesis, they assume
	Contribution:	The main concern is on layer 4	if the frame contains a relevant	relevant object, the frame will be considered as non-critical.	that it is possible to detect corner cases
	<ul> <li>a formal definition of a corner case</li> </ul>		moveable object (e.g., pedestrian,		with a camera-based system.
			vehicle, bicycle, etc.) and its critical	A corner case score is calculated  A corner task (1) the difference have an	1 to the stand
	in a video stream;		score is higher than a threshold.	according to (1) the difference between	Limitation:
	domain-specific challenge		score is higher than a threshold.	the predicted image and the actual	Within this work, they limit themself to
	identification regarding corner		The critical score will increase if (1)	frame; and (2) the distance between the	mobile objects, which determine the
	case or anomaly detection in a video stream;		this frame is largely different from	relevant object and the ego vehicle.	relevant classes for corner case
	,		a predicted frame (based on	If the corner case score exceeds the	detection.
	Propose a system framework for corner case detection in a video		previous frames by a given image	threshold, a corner case is detected.  The score and the location of the	
			prediction algorithm); and (2) the		
	stream.		relevant object is close enough	relevant object are outputted.	
			(comparing to a given threshold)	To identify the location of the relevant	
			to the ego vehicle.	object, they simply assume that objects	
				being farther away from the bottom of	
				the image are farther to the ego vehicle.	
[65]	Activity: Criticality assessment	Definition of critical scenario is not explicitly given	The purpose of this paper is to	Input:	Required knowledge(s):
[65]	Activity. Criticality assessment	in this paper.	assess the ability of CV algorithm	Light modelling	CV algorithms (YOLO and Faster
	Phase: Component design /	in this paper.	to detect an object with different	3D car modelling	RCNN)
	verification	Covered layers: 5	color in the different light	I -	Generated photorealistic virtual world
	vermeation	covered layers. 5	conditions.	Environment modelling	Five common colors for virtual car
	<b>SOI:</b> CV function	In this paper, they generate scene (i.e., picture)	Conditions.	Output	
	Joi. ev function	with various light conditions (environment	Based on our understanding, the	Output:  • Photo realistic virtual world with a 3d	(i.e., black, white, red, blue, green)
	Motivation:	conditions) and car colors to assess CV-based	critical scenario could be		Intensity of illumination from low     (0.001 refers to dark condition) to
	This paper tries to assess a CV	vehicle detection algorithms.	happened when the CV algorithm	sedan car as a main object.	(0.001 refers to dark condition) to
	algorithm (YOLO and Faster RCNN) by	vernole detection dispondings.	fails to detect an object (i.e., sedan	Process of generating photorealistic	high (400 refers to very bright
	generating a photorealistic virtual		car in this paper)	virtual world:	condition)
	world.		ca. iii alis paper)	virtual world:	Evaluation process:
			1		Evaluation process.

	In particular, they tried to reproduce various illumination intensities in their photo-realistic virtual world scene. Then, based on the reproduced scene, they conduct assessment for two CV algorithms to detect a sedan car with different colors.			First, they conducted an accurate light modelling. Light is essential part to generate a photorealistic virtual world since it can affect or determine appearance of the object in the environment. And in particular, they tried to capture the different behaviors of light that arise from nature.  Second, they created a 3d car by using 3ds Max as the modelling software. The car is made with 203,522 polygons and 610,556 vertices.  Third, they used Unreal Engine 4 (UE4) to create an environment/scene modelling. They used diffuse bidirectional reflectance distribution function (BRDF), Microfacet Specular BRDF, and environment BRDF as for lighting system.	In this paper, they evaluated the CV algorithms based on various intensities of light. Moreover, they tested the capability of algorithms to detect car colored with common color that are mentioned in the required knowledge.  The results show car under very high condition can hardly be detected.  Moreover, cars with red and blue color are more robust to the variation of illumination.
[66]	Activity: Assessment / validation	Covered layer(s): 2 and 5	They defined critical scenarios as corner cases.	Input:  Image belonging to class A (nominal	Required knowledge(s):  Three image datasets
	Phase: Component design	This paper generated corner cases based on "stop" sign images. And the images are transformed	And CV algorithm is validated by	condition)  Image belonging to class B (corner	Information regarding important features of corner case image (e.g.,
	<b>SOI:</b> Sign detection function	based on the various temperatures (e.g., room temperature, high temperature). Thus, the	its capability to detect stop sign. If the CV algorithm cannot be able to	case)	the mosaic noise textures used by high temperature or distortion
	Motivation:	covered layers are the road infrastructure and	detect the sign, then it could lead	Output:	patterns caused by rain drops).
	This paper tries to automatically generate corner cases by using their	environment conditions.	to critical scenario.	Image belonging to class B (corner case).  Specifically, the expected output is a	Three high temperature datasets.
	proposed method named cycle-			corner case image that appropriately	One normal temperature dataset.
	consistent generative adversarial			carry the important feature of "corner	
	networks (CycleGANs). And the			case" while retain other fundamental	Evaluation process:
	generated corner case images are used to validate the robustness and			characteristics of image (e.g., sizes and	They evaluated the proposed method by
	reliability of ADAS to ensure the			shapes of background objects).	using three datasets as follows:
	safety.			Process of generating corner case	Full dataset including 164k high- temperature images.
	,			images	Small dataset including 2k high-
				-	temperature images.
				Generator structure:	_

The main reasons are to minimize the	Encoder: It consists of convolutional     Hybrid dataset including 2k high-
effort and budget for physically	layers. It aims to extract from a given temperature images and 162k
collecting data.	image using CNN. synthetic images.
	Transformation: Based on ResNets to
	achieve accurate refinement for
	feature extraction. It aims to modify  The results showed that the generate
	the extracted features. synthetic images have similar features
	Decoder: It takes the modified feature the actual images. Moreover, the
	after transformation and generates synthetic images retained the importa
	the corresponding image from these characteristics of nominal recordings.
	features. It consists of
	deconvolutional layers.
	deconvolutional layers.
	Training the generator:
	It is challenging to train the generator to
	generate corner case automatically. In
	this paper, they used CycleGANs, and it
	consists of four major components as
	follows:
	Forward generator: It aims to
	generate synthetic images that are
	identical to real one.
	Forward discriminator: It is created to
	guide the training of forward
	generator. It is designed to judge
	whether a given corner case is real or
	synthetic.
	Backward generator: The function of
	backward generator and backward
	discriminator are to prevent the
	multiple input images to be mapped
	to the same output image. In
	particular, backward generator the
	inverse transformation of the forward
	generator.
	Backward discriminator: It aims to
	distinguish between real and
	synthetic nominal recordings.

[67]	Activity: Assessment / validation	Covered layer(s): 4 and 5	The definition of critical scenario is	Case study 1:	Required knowledge(s):
			not explicitly given in this paper.	The AEBS determines a braking mode	• Images.
	Phase: Component design	This paper generated scene with different intensity	However, the critical scenario	depending on the speed of vehicle (vs),	Values to define counterexample
		of object color and rotation of the object. They	could be happened when the CV	its velocity (vp), and the distance	candidates.
	SOI: CV / ML function	also displaced the object to different location.	algorithms fails to detect the	between vehicle and the obstacle (dist).	
		Hence, the covered layer is movable objects and	object.	Then, the AEBS will compute the times to	Evaluation process:
	Motivation:	environment condition.		collision and longitudinal safety indices	They validated the DNN algorithms by
	This paper tries to find falsifying			(e.g., safe, warning, braking, collision	using the corner case misclassifications
	executions, such that, they will know			mitigation mode).	identified from the steps that are
	whether the output from learning				mentioned in the previous column.
	components can lead to a failure of			First, they tried to find the region of	
	CPS.			uncertainty (ROU) where they identify it	Note: Use case 1 is out of the scope of
				as counterexample candidate. The ROU	literature study.
	They conducted two case studies in			found when vs= 25 and dist= 40.	
	which the first case study is				
	conducted based on Simulink for			Then, they generated an image that can	
	advanced emergency braking			lead to misclassification by changing the	
	systems (AEBS) that connected to			brightness and location of the object.	
	DNN-based image classifier.				
	In their second case study, they			Case study 2:	
	conducted a validation for a CNN			In this case study, they implemented	
	algorithm to detect a cow in a self-			CNN that classifies the pictures captured	
	driving simulator. If the algorithm			by the onboard camera in two	
	fails to detect a cow, the car will			categories, e.g., cow and not cow.	
	collide with the cow.				
				Then, they try to misclassify the scene by	
				changing the rotation of cow and the	
				color of cow.	
				Based on this case study, they tried to	
				find a case where the AEBS fails to	
				operate.	
[68]	Activity: Assessment	Definition of critical scenario is not given in the	No critical scenario is addressed in	Input: extracted images from videos.	Required Knowledge:
		paper.	this paper.		1. Image dataset
	Phase: Component design /			Output: lane detection with marking	2. DNN algorithms
	verification	Covered Layers: 1, 2, and 5.	However, we can assume the	annotations (e.g., white dashed line is	
			critical scenario could be	annotated light yellow, yellow single line	Evaluation process:
	SOI: CV function		happened if the LD systems cannot		-

	Motivation: This paper establishes the reference systems to evaluate the quality of line marking built by transportation agencies to support ADAS functions that rely on pavement markings.  Also, the test system can be used by developers as benchmark for their proprietary systems.  They gathered an extensive video dataset of various roads in Central Texas at different times of day and weather conditions to support the proposed test system.  Out of the scope	In this paper, they evaluate the line detection algorithms performance based on the environmental factors, lane marking types, color, material, and the retro reflectivity of pavement markings. Also, the dataset they created includes different types of roads (e.g., asphalt and concrete road surfaces)	detect the line marking when it is activated for ADAS.	with orange color, and road curb with yellow color)  Process of gathering the Dataset: The video data were gathered in various roads at different times of day (morning 11 am CST, evening 6 pm CST, and night 10 pm CST). To maintain the homogeneity of the video, the camera was set at 25 fps during the recording of roads.  Moreover, they used retro reflectometer to measure how visible the marking will be at night.  DNN-based LD algorithms they tested:  1. SCNN 2. LaneNet 3. ENet	They used Scalable tool to annotate each image in dataset. However, they still annotated the image manually. The performance metric they used is based on conventional pixel-accuracy such as True Positives (TP), False Positive (FP), F-Measure, etc.  In particular, they set a threshold for line markings with the width equal to 30 pixels to evaluate whether the line marking is successfully detected.  Limitation: The annotation of each image is given manually.
[69] CV- HAZ OP	Activity: influential factor analysis Phase: Requirement analysis, component design SOI: CV function  In this paper, a complete HAZOP is conducted on a generic CV system for automated driving.  The result is a checklist with more than 900 identified hazards (it is called hazard in the paper, but it actually means failure mode). The checklist can be used to evaluate and improve test datasets.  This paper is out of the scope of the survey.	Scenario and scene are not explicitly mentioned in this paper.  According to our interpretation, a scene in this paper includes the content of the image captured by the camera and the whole perception system including sensors and algorithms.  Covered layers: 1,2,4,5 and the potential problems of the CV functions of the ego vehicle. It covers all the items that need to be identified/classified by the CV functions.	The purpose of the HAZOP is to analyze how different deviations from the design intent of the CV system will lead to perception information loss (i.e., the definition of hazard in this paper).  Example of loss of information: A glare may cause a loss of texture information.	HAZOP performed by CV experts and safety experts on the whole CV process.  The whole CV process is divided into 5 nodes (or locations in the paper's term), namely light sources, medium, object, observer and algorithm. Different parameters are defined for different nodes.  Generic key words and CV-specific additional key words are used.  A deviation is identified by a combination of a node's parameter and a keyword.  The consequences of the identified deviations are judged and reviewed by	Required knowledge:  1) Knowledge of CV systems.  Validation:  1) Expert validation to check the relevance of the identified hazards (i.e., information loss)  2) They use stereo vision as a case study. For the identified hazard "no texture", failure rate at the identified hazardous area (where "no texture applies") on a picture is higher than the average failure rate for various algorithms on multiple databases.  The hardware running the algorithms is not included in this paper. Therefore, it only considers SOTIF problem but not ISO 26262.

		multiple experts with different	
		backgrounds.	

Table 6. Deductive reasoning methods

#	Purpose	Scenario definition	Criticality definition & Surrogate Measure	Solution	Other key observations
[34]	Activity: Reasoning	This paper only considers highway	A critical scenario should contain at least	This paper proposes a qualitative and	Required knowledge:
	Phase: system validation	scenarios. The scenario definition includes	one accident threat (i.e., one accident	systematic approach to derive the	1) Potential behaviors of vehicles on the
	<b>SOI:</b> the whole system	(1) the relative positions between the ego	type may potentially happen)	scenario catalogue.	highway
	ODD: Highway	vehicle and the threatening vehicles; and			2) Possible collision types
		(2) the intended maneuvers of the ego	This paper assumes three types of	The approach starts with basic critical	3) Traffic rules on the highway.
	It provides a systematically defined	vehicle and the threatening vehicles.	accidents from the perspective of the ego	scenarios, where only one threatening	
	test case catalogue with good		vehicle, namely rear-end collision, front-	vehicle is considered, and the ego vehicle	Validation:
	coverage of critical highway traffic	All the vehicles have only two types of	end collision and sideswipe.	has only one intended maneuver (lane	1) The coverage of the identified test
	situations. Each entry of the	maneuvers, namely lane keep (accelerate,		keep or lane change). Nine basic critical	case catalogue is evaluated by a
	catalogue is one functional scenario.	decelerate, keep speed) and lane change	In this work, a scenario starts from a	scenarios are identified.	naturalistic driving behavior database.
		(steer left and steer right). A complex	threat-free condition and ends with either		2) One entry is parameterized and
	The goal of this catalogue is to cover	maneuver will be a combination of these	a crash or another threat-free condition.	When encountering an accident threat,	sampled to get concrete scenarios for
	all the pre-crash scenarios on a	maneuvers.		the ego-vehicle may start an evasive	simulation, so as to identify the
	highway.		In other words, this work tries to	maneuver (brake, accelerate or lane	performance boundary of this entry.
		Covered Layer: 4	catalogue all the pre-crash scenarios.	change), which may lead to a secondary	
				accident threat. These scenarios with	
				evasions are called complex scenarios.	
				One complex scenario can be seen as a	
				connection of multiple basic scenarios	
				with evasive maneuvers. In total, 13	
				complex critical scenarios are identified.	
				When identifying complex critical	
				scenarios, they limit the number of	
				threatening vehicles within 3 and the	
				number of evasive maneuvers within 2.	
[70]	Activity: Reasoning	The paper mentioned the six-layer scenario	A scenario is critical if it may lead to a		Required knowledge:
	Phase: system validation	model. It says that in this work, only the	collision.	Critical functional scenarios are identified	1) Potential behaviors of vehicles on the
	<b>SOI:</b> the whole system	movements of objects (i.e., the layer 4) are		through a qualitative and systematic	highway
	ODD: highway	considered.	Each critical scenario is described by the	approach.	2) Possible collision types
			collision type and the initial position of the		3) Traffic rules on the highway.
	This paper introduces a framework to	In this paper, a base scenario shows how	challenging vehicle.	First, it defines all the possible ways to	
	define safety relevant functional	other vehicle (challenger) may collide with		collide between two vehicles on a	Validation:
	scenarios, i.e., scenarios ending up	the ego vehicle assuming the ego vehicle		highway.	No validation
	with a crash.	keeps its lane and speed.			

	It emphasizes that by only considering relevant objects (e.g., the vehicles close to the ego vehicle) the number of possible scenarios can be significantly reduced.	Covered layer: 4		Second, it considers other situations that may increase the challenge to avoid the crash, e.g., the evasive trajectory is blocked by a third vehicle.	So far, they only considered the collisions that involve only two vehicles.
[71]	Activity: Reasoning Phase: system V&V SOI: The whole system  The purpose of this method is to identify and quantify hazardous scenarios for highly automated driving vehicles with an emphasis on AD function limitations and failures.	In this paper, a scenario is defined as the temporal development between several scenes in a sequence of scenes. However, the necessary content in a scenario description is not given.  According to our interpretation, the hazardous scenarios include a hazard and the environmental condition, which may trigger the hazard.  Covered layers: (1, 2), 4, 5 + hazard of the ego vehicle	This paper uses the term hazardous scenario, which refers to a scenario that may lead to a harm, caused by the functional limitation or failures of the system.	Hazardous scenarios are identified with the following steps: Step 1 is to model the automated driving functions as components and interfaces  Step 2 is to identify hazards. They firstly identify generic vehicle-level hazards that are independent of the underlying implementation with a HAZOP-like method. Secondly, they identify the Functional Insufficiencies with a HAZOP-like method. Here, each AD function is treated as a black box.  Step 3 is to identify the causes of the functional insufficiencies and the corresponding environmental conditions with "environmental fault tree" (a new method proposed in this paper to combine triggering condition with fault tree).  Step 4 is to quantify the risk of the identified hazardous scenarios (functional insufficiencies + environmental condition)	Required Knowledge for the identification of the generic hazards (step 2.1)  1) A set of base (pre-crash) scenarios (e.g., the ones identified in [70])  2) A set of predefined basic maneuvers (e.g., start, follow, turn left/right)  3) A set of keywords to determine possible Incorrect Vehicle Behavior  4) A set of top-level events (e.g., collision types)  5) Possible behaviors of vehicles on the road  Required Knowledge for the identification of the generic hazardous scenarios (steps 2.2 & 3)  1) Interfaces of each AD function  2) A set of predefined key words to determine Functional Insufficiency  3) A set of basic scenarios  4) Understanding of the system and functions to analyze the causes of each functional insufficiency  5) Influential environmental factors
[72] <i>,</i> [73]	Activity: Deductive reasoning to generate test case Phase: Function validation/evaluation SOI: adaptive cruise control, active lane changing control and active lane keeping control for L2 function.	The scenario includes:  • structured road (straight, curved and ramp sections of urban road and highway)  • ego-vehicle and its intension  • intension (9 possibilities such as going straight, left/right lane change, left/right	The scenario importance is used as main criteria to judge the test value of the designed test scenarios. The author defined four level form to classify the scenario importance based on their	Input: function features analysis and specified traffic condition.  Output: valuable test scenarios (logical scenario)  Method:  Step1: define road structure and condition of the ego vehicle	Required knowledge: - Function feature Validation: the coverage of generated valuable scenarios was validated with test regulations of level 1 automated vehicles, the relevant traffic accidents database, the classification of test

-		T	T .	T	T
	<b>ODD:</b> straight, curved and ramp	lateral moving, and left/right U turn) and	impact on the ego-vehicle's movement	Step 2: analysis of the scenario	conditions defined by some projects
	sections of urban road and highway	relative position (in the paper the author	(longitudinal and lateral movement.)	importance with one surrounding vehicle	(EuroNCAP (AEB), ISO (ACC), NHTSA,
	This paper presented a deductive	uses 8 possible positions around the	<ul> <li>Level A: possible collision</li> </ul>	(define corresponding levels from A to	Waymo, ADaptIVe and GES 2015)
	method of testcase generation for	ego-vehicle) of surrounding vehicles.	Level B: longitudinal and lateral	D), scenarios with an importance degree	
	the function validation.		movement impact	of D have no test significance and were	
		Covered layers: 1, 4	Level C: longitudinal or lateral	excluded.	
			movement impact	Step 3: adding another vehicle to the	
			Level D: no impact	identified valuable scenarios by step 2 to	
			Levels A, B and C are considered as	form new scenarios and analysis of the	
			valuable scenarios.	scenario importance	
			Tanada e seemanesi	Step 4: adding more vehicles analog to	
				step 3.	
				If the impact of detection and response	
				of ego-vehicle interfered by the	
				movement of multiple obstacle vehicles	
				in the higher-level scenarios is same as	
				the that of lower one level scenarios with	
				one less obstacle vehicle, those higher	
				scenarios are no longer considered as	
				valuable scenarios.	
[74]	Activity: Deductive reasoning	The authors only proposed a framework.	In this paper, they proposed two concepts,	Input: the logical scenarios will be taken	Required knowledge:
	method to refine the given logical	No concrete scenario model was proposed.	complex scenarios and critical scenario.	from: laws, regulations and system	System specification, specific driver
	scenario		This paper uses TTC (Time-To-Collision) as	specification	safety training information and driving
	Phase: Function validation		a metric for the criticality definition using	Output: relevant concrete scenarios	license directive, understanding of
			simulation.	According to the methodology first the	complex scenarios
	This paper proposes a methodology		The following factors are considered to	logical scenarios are taken from three	
	for an intelligent selection of relevant		increase the complexity of the logical	sources.	<b>Limitation:</b> With the method presented,
	scenarios for the certification of		scenario:	They proposed a two-stage optimization	it is not possible to determine all
	automated vehicles.		Number of elements	framework to generate concrete	parameters of the five layers model
	The aim of this paper enables the		Number of states per element	scenario. A detailed optimization method	precisely, because it is not entirely
	technical service to carry out		Interdependency	was not proposed. In the first	possible to determine the relevance of a
			Self-dynamics	optimization stage the parameters of	parameter for a scenario.
	scenarios that are relevant from its			1	The constant of the colonial decreases
	perspective, thus preventing so-			layer one, two and five (refer to 5-layer	The method developed does not cover
			Intransparency	layer one, two and five (refer to 5-layer model) are first optimized by sensor	the entire parameter space there is no
	perspective, thus preventing so-		<ul><li>Intransparency</li><li>Multiple conflicting goals</li></ul>		· ·
	perspective, thus preventing so- called gaming of tests, and at the		<ul><li>Intransparency</li><li>Multiple conflicting goals</li><li>Openness of the target situation</li></ul>	model) are first optimized by sensor analysis and consideration of driving	the entire parameter space there is no
	perspective, thus preventing so- called gaming of tests, and at the same time perform an efficient		<ul><li>Intransparency</li><li>Multiple conflicting goals</li></ul>	model) are first optimized by sensor	the entire parameter space there is no guarantee that all errors of the SUT will

		objects are defined (to refine the logical	
		scenario) by considering complexity and	
		their trajectories are optimized.	

Table 7. Inductive reasoning methods

#	Purpose	Scenario definition	Criticality definition& Surrogate Measure	Solution	Other key observations
[75]	Activity: Reasoning	The purpose of this paper is to find critical	In this paper, a critical scenario means a	Input: textural accident database (detailed	Required knowledge:
	Phase: design + V&V	functional scenarios. In their example	crash scenario.	functional scenarios)	Crash scenario database
	<b>SOI:</b> the whole system	method, a functional scenario is a template		Output: critical functional scenarios	
		sentence to combine the identified high-	The proposed method also defines a scope		Validation:
	This paper proposes a method to	frequent wordings, or a variance of this	for the CSI. E.g., in this paper, the scope is	In the database, information for each	This proposed Big Data technique-
	identify critical scenarios from	template sentence.	urban scenarios.	scenario includes time, location, vehicle and	based method is validated in
	textural accident database through	The template sentence in this paper is "A		driver details, before-crash maneuver,	comparison with the resulting test
	text-weight analysis.	crash is likely to occur when 'maneuvers'		triggering events, crash descriptions of	scenarios from a manual investigation
		during 'traffic operations' at 'crash		police officers, etc.	of crash data, and it was found that 14
		location' due to 'triggering event'."" Where			of a total of 18 scenarios correspond
		the words in " needs to be replaced by one		Process:	to the scenarios from manual
		wording in the corresponding category.		1) Scenarios in the database are first	investigation and the other four
				filtered according to the scope of	scenarios are additionally derived by
				interest (e.g., urban scenarios).	the proposed approach.
				2) Text weight analysis (searching for	
				frequent wordings)	
				<ul><li>3) Select the high-frequent wording</li><li>4) Categorizing wordings by types</li></ul>	
				5) Scenario developments as descriptive	
				sentences based on the sentence	
				template.	
[76]	Activity: generating critical concrete	Covered layers: 1, 4, 5	A scenario is critical if in the simulation,	Input: accident database (set of functional	Required Knowledge:
_	scenarios from accident databases		the ego vehicle (i.e., the system under	accident scenarios)	1) Accident database (NHTSA)
[78]	(functional scenarios)	In this paper, a scenario is defined based	test) cannot avoid the accident extracted	Output: a set of concrete critical scenarios	2) A simulator (BeamNG.research)
AC3	Phase: V&V	on a given topology, which contains the	from the accident database.		3) Model of the SOI as a black box.
R	<b>SOI:</b> the whole AD system	environment (weather, lighting, and		Simply speaking, this approach has three	
		roads), the traffic participants and their		steps:	Validation:
	This paper proposes a method to	actions (e.g., movements), as well as the		Parse each accident description	The approach is validated from 4
	parse each entry of an accident	accidents.		according to a pre-defined scenario	perspectives:
	database to transform it into a			ontology with Natural Language	1) How many simulations can be
	simulation scenario for the purpose			Processing (NLP) techniques.	successfully generated from
	of test case generation.			2) According to the parsed information,	accident descriptions? This is
				generate simulations which can	answered by checking if a
				represent the accident scenarios	simulation can be generated from a
				depicted in the database. Trajectories of	description and comparing the

				dynamic objects are modeled as a vector of way points.  3) Replacing one vehicle in the simulation with the ego-vehicle and check if its behavior passes the oracle, which is to safely reach a goal point within a given time. The goal point is behind the accident point to guarantee that the ego vehicle avoids the accident.	simulated damage with the recorded damage.  2) How well the generated scenarios represent the description? This is answered by an empirical study, people are asked to read the description and the generated simulation videos to provide comments.  3) The computation time for simulation generation is acceptable.  4) They compare the critical test cases generated by AC3R with non-critical test cases in terms of code coverage and neuron coverage and critical scenarios outperform non-critical ones.  5) The effectiveness of AC3R is validated by comparing the test results on critical scenarios and non-critical scenarios in terms of fault (unavoidable crashes) detection.
[79]	Activity: Inductive reasoning method	Covered Layers: all layers (qualitative	A trajectory is critical if it leads to a	Input: a set of concrete scenarios	Required knowledge:
	to generate critical scenario	analysis)	collision or an unfinished task.	Output: the minimum group of scenarios	- Logical scenario
	Phase: System verification			covering the test content of the initial	- FTA analysis
		The scenario is defined by SCPs (scenario	A scenario is critical if there exist a	scenarios	
	This paper proposes a scenario analysis and simplification method	characteristic parameters). The SCPs include qualitative parameters and	possible critical trajectory. In other words, a scenario is critical if it is possible to have	Method:	No validation available in paper.
	for reducing the number of test	quantitative parameters.	a collision in this scenario due to FuSa or	First, input the concrete scenarios set that	
	scenarios for HAV test and	Quantitative parameters: the number of	SOTIF problem of the ego vehicle.	needs to be analyzed. Then, by analyzing	
	evaluation.	interfering vehicles, the initial position and	,	concrete scenarios through the traversal of	
		initial speed of each interfering vehicle, the		trajectories, trajectories which lead to	
		initial position and initial speed of the VUT,		collisions or test tasks uncompleted are	
		the number of lanes, and the curvature of		obtained. By analyzing these trajectories,	
		the lane.		the SCPs of the corresponding scenario are	
		Qualitative parameters: vehicle type		obtained using functional decomposition [80], combined with the fault tree analysis	
1 1	l l				
		(passenger or commercial vehicle), road facilities conditions (such as if road		(FTA). By analyzing the overlap or contain	

		unobstructed), lighting conditions (normal lighting, backlighting, streetlights, darkness, etc.), weather conditions (sunny, fog, rain, snow, etc.), road conditions (dry, stagnant water, snow, ice, etc.).		relationship among scenarios are obtained according to the SCPs included in different scenarios. By searching for the combination that contains the fewest scenarios but still cover all the SCPs and use this set of scenarios to replace the original combination of test scenarios, the redundant evaluation scenarios were deleted. Therefore, this method further reduces the number of test scenarios.	
[81]	Activity: Inductive reasoning to generate pre-crash scenario from accident data base Phase: Function validation SOI: Autonomous Emergency Braking (AEB) system.  This paper presented an inductive method (based on scenario clustering) of testcase (logical scenario) generation for the AEB system based on the accident data.	The scenario description in the paper includes environmental parameters, static parameters, and the dynamic parameters of traffic participants. The paper presented 11 fields related to scenario features: subject participant, object participant, accident type, collision type, road type, road condition, road separation, light condition, weather condition, participant type, speed.	In this paper, critical scenarios refer to potential accident scenarios.	Input: Accident data Output: Set of typical pre-crash (logical) scenarios First, data from the IGLAD database were analyzed and divided into four categories based on differences in traffic environments among countries and regions. In each group scenarios were clustered. Clustering method: • Feature selection: after a comparative analysis 11 fields related to scenario features were presented • Feature representation using concept of "flip distance" • Clustering analysis using SPSS One typical scenario was chosen in each cluster. Chi-square was used to select typical scenario. If an actual chi-square value was found to be greater than the standard value, the value of the variable was considered significant, and a variable with a high proportion was selected as a scenario element. Otherwise, a variable with a large number was selected as a scenario element. In total 21 typical pre-crash scenarios were found.	Required knowledge:

[82]	Activity: Inductive reasoning to generate test case from accident data base  Phase: System design  SOI: Collision Warning System at intersection.  This paper presented an inductive method of testcase generation for the Collision Warning system based on the accident data. The corresponding scenarios were the collision between two vehicles at the intersection.	Main data source for this study is from Naturalistic Driving Study (NDS), a database developed by a research project Second Strategic Highway Research Program (SHRP2) which is supported and operated by the Virginia Tech Transportation Institute (VTTI). 16 scenario classes were defined according to the intentions of two involved vehicles.	This paper uses Safety- remaining distance (SRD) for the scenario evaluation. It is based on the concept of safety stopping distance, as a quantitative indicator to measure their performance.	Input: Accident data (two sensor system: camera-based and radar-based data)  Output: evaluation of the two sensor systems under 16 predefined pre-crash scenario classes  The author first selected 363 accident scenarios from two sets of intersection accident data.  All these selected scenarios were classified into sixteen vehicle-to-vehicle pre-crash classes. Corresponding SRD were calculated to each scenario for two sensor system. If the SRD is greater than zero, it means that it is possible to prevent an accident.  Prevention rate of each system in different scenario class was calculated. The prevention rate was then compared with	Required knowledge:  Accident data from Naturalistic Driving Study (NDS)  16 pre-crash scenario classes at  No validation.
				the compliance rate of each scenario to evaluate which sensor system is necessary for each scenario class.	
[83]	Activity: Inductive reasoning to generate test case from accident data base  Phase: Function validation  SOI: Autonomous Emergency Braking (AEB) system.  This paper presented an inductive method of testcase generation for the AEB system based on the accident data.	The scenario features in the paper include: Time, Time of crash, obstruct, visual obstruction, intention of car, pre-crash driving behavior of the car driver, intention of the TW and pre-crash driving behavior of the TW driver.	Pre-crash scenarios	Input: Accident data Output: Six typical car-to-TW (two-wheels) scenarios.  Clustering method: • Feature selection: five features were selected according to experience • Correlation analysis between the features was calculated to show that the selected features were independent enough for clustering. • K-modes method was applied to cluster the scenarios in the databse.  Medoid scenarios (i.e., the typical scenario in each cluster), created from clustering algorithm, were combinations of these five crash characteristics.	Required knowledge: Accident data  Validation: The found six typical pre-crash scenarios were compared with the EuroNCAP AEB 2018 scenarios. The scenarios identified by the author covered all the scenarios in EuroNCAP. Furthermore, the identified scenarios included scenarios in which the car or the TW was turning, while Euro NCAP scenarios only include cars or the bicyclist moving straight ahead.

[84]	Activity: Phase: Function verification ODD: urban or motorway SOI: ACC, AEB and LKA  This paper presented a systematic approach for assessing the effectiveness of ADAS using accident data.	In this paper a concrete scenario is an entry of GIDAS PCM (precrash matrix), which contains information on environment and vehicle dynamics for the precrash phase of 5 s before the first impact for selected GIDAS cases.	Criticality KPIs: Time gap (longitudinal front vehicle distance divides ego vehicle velocity) for ACC TTC (time-to-collision) for AEB TTLC (time-to-line-crossing) and DLC (distance-to-line crossing) for LKA  Green spots: the situation can be solved by the system.  Grey spots: the situation cannot be solved by the system, unless system boundaries can be extended.  White spots: The situation cannot be addressed by the system in either basis or extended configuration.	Input: Accident database Output: set of concrete critical scenarios  The author first selected scenarios from the accident database based on injury severity score (> 2.5). The selected scenarios were then simulated to calculate criticality KPIs. Three classes (green, grey and white spots) were categorized based on the simulation results.	Required knowledge:  Accident data (GIDAS PCM)  A simulator (rateEFFECT)  System as black-box  No validation.
[85]	Activity: Inductive reasoning method to generate concrete crash scenario Phase: Function V&V ODD: urban traffic  This paper proposes a method based on Microscopic Traffic Simulation to obtain a large number of urban traffic scenarios.	Scenario on microscopic traffic level (position, x,y speed. posLat, speedLat)	The Scenario Risk Index calculation: the magnitude of risk is equal to the probability of a risk event times the degree of loss. The loss calculation was based on the kinetic energy of collision.	Input: public traffic data for MTS (microscopic traffic simulation) parameterization Output: concrete crash scenarios  Method described in the paper: 1. Using public data to calibrate the traffic simulator. 2. Perform simulation. 3. Data postprocessing of the simulation results to extract the concrete crash scenarios. Each vehicle in the simulation is regarded as Ego. The calculation of SRI (scenario risk index).	Required knowledge:  • Traffic data  • SUMO  No validation.
[86] VAA FO	Activity: creating the database of critical concrete scenarios  Phase: the database can be used for statistical validation / system verification  SOI: the whole AD system  Virtual Assessment of Automation in Field Operation (VAAFO) tool runs in parallel with human driving. It	In this paper, a scenario is defined by all the sensor data collected by a humandriving vehicle. The vehicle is equipped with all the sensors that the AD function needs. The logged sensor data will be processed off-line to represent the real world more correctly. The corrected world model incudes constant objects and the behaviors of the dynamic objects.	The logged decision made by the AD function during runtime will be mapped to the corrected perceived world model.  The paper says that for the assessment module, the simplest measure is whether a real collision has occurred or not. Further, multiple metrics for preventive or active safety can be implemented. Those can range from the safety in the current	Input: human driving Output: critical concrete scenarios  The AD functions make decisions based on the on-line world model and this decision is verified on the corrected world model.  The AD function may make a decision that is different from the human driver's. This difference may consequently affect the	Required Knowledge: 1) Human driving sensor data 2) Simulator running online to calculate the planned behavior of the AD functions.  Validation: not mentioned

	perceived world. The trajectory planned by the AD functions is compared with human driving	The perceived world model (after off-line correction) is more accurate than the online version because:  1) Further measurement can be used.  2) More complex sensor fusion algorithm can be used since there is no time limit for computation.  3) The driver is in the loop to correct manually.  The AD function is making decision during runtime based on the sensor inputs. Its decision is also logged.	motion state (TTC, constant reserve time, etc.) to motion prediction models (physics-based, maneuver-based, and interaction-aware). However, no particular metrics are given.	behavior of other vehicles. To solve this, VAAFO shorten the duration of each simulation to 2 seconds, and a new simulation is initiated every 0.5 second. VAFFO assumes that the behaviors of other vehicles will not be significantly affected by a different decision made by the AD within 2 seconds.	
[87]	Activity: Refinement of concrete scenarios Phase: System verification SOI: The whole system  The purpose of the study is to generate new collision scenarios from already recorded ones.  For that, the authors propose to train Recurrent Neural Networks (RNNs) to generate new collision scenarios.	Covered layer: 2, 4  They use "speed and direction of vehicles for in-vehicle data and traffic light data to represent V2X data".  Layer 4 is represented by the speed and direction of other movable objects.  Layer 2 is represented by the traffic light data  They mention V2X data, which would be layer 6, but they only use traffic light information.	In this study they only consider scenarios where there is a collision.  They do not consider a specific system under test for this process. The aim of the study is to generate new accident scenarios from prerecorded data using a RNN.	Input: A set of concrete scenarios Output: A set of generated concrete scenarios  To generate new collision data from prerecorded data using ANN, they use Long Short Term Memory Networks (LSTM). The data used to train the network comes from a simulation environment, but it could be real accident data. In the example developed in the study, the data includes speed, direction of vehicles and traffic light data.  Once trained, the network can be used to generate new collision data starting from an initial seed that contains the initial speed, direction and traffic light state.	Required knowledge:  Recurrent neuronal networks (RNNs)  Accident data or a simulator to generate accident data  Validation: The generated scenarios are compared with the original scenarios in terms of:  The distance travelled from both vehicles.  The total speed at collision from both vehicles.  The cumulative angular change from both vehicles.

Table 8. Formal methods

#	Purpose	Scenario definition	Criticality definition& criteria	Solution	Other key observations
[88]	Activity: Formalization & criticality	Definition of scenario is not explicitly given in	Criticality is defined based on the	Inputs: Executable (logical scenario)	Required knowledge:
[00]	check	the paper.	formally defined scenario	model for model checking	Behaviors and reactions of other
			specifications.	Output: pass or a counter example (a	vehicles
	Phase: requirement analysis	Our Interpretation:	'	simulated scenario)	2) Specifications of the decision making
	(verification) or component design	A scenario is defined by the lane structure and	Critical scenarios are the ones where	·	and control functions.
	(early-phase specification	the behaviors of all the involved objects.	the AD function cannot satisfy the	Scenario specifications are modeled as	3) Dynamic model of the ego-vehicle
	verification)		corresponding scenario specification.	traffic sequence charts. The behaviors of	4) Lane structure of the road
	SOI: the decision-making function	A scenario catalog is defined by the lane	(According to our understanding,	all the objects and their interactions with	5) Scenario specifications
	(implicit)	structure and all the possible behaviors	scenario specifications can be either	the ego vehicle are modeled as hybrid	
	ODD: structured road	(including interactions with other objects) of	functional requirement or safety	automata. These two are input to a	Validation:
		objects other than the ego vehicle. This is the	constraints)	model checker, which consequently	No Validation
	At requirement analysis phase, this	closest definition to logical scenario.		evaluates if the AD function of the ego	
	method can formally verify if the		The AD function needs to be modeled	vehicle satisfy all the scenario	
	specifications of the AD functions are	Scenario specification: A formal way to model	(maybe simplified) as a hybrid	specifications. If not, a critical scenario	
	safe within the predefined scenario	acceptable behaviors of the ego vehicle within	automaton.	will be returned.	
	catalogue. If it is not safe, a counter	a scenario catalog.			
	example (i.e., a critical scenario) will			Model checking can guarantee full	
	be provided.	Covered layers: 1 (fixed for each logical		coverage on the parameter space.	
[00]		scenario),4 (including the ego vehicle)			
[89]	Activity: Instantiation & criticality	Covered layers: 1,2 (traffic laws),4	A critical scenario is a concrete	Inputs: Executable (logical scenario)	Required knowledge:
	check (falsification)		scenario where the ego vehicle violates	model for model checking	1) Behaviors of other traffic objects
	<b>Phase:</b> early-phase component verification	In this paper, a logical scenario contains the road structure (including the possible	the traffic laws.	Output: pass or a counter example (a	modeled by a hybrid automaton. 2) The decision making and control
	<b>SOI:</b> Decision making + motion	variation), the behavior models of the traffic		simulated scenario)	algorithms of the ego vehicle modeled
	planning + control	objects (including the ego vehicle), The traffic		The falsification process:	in a hybrid automaton.
	planning + control	laws, the goal of the ego vehicle (i.e., its		The formal scenario models will be	3) The falsification tools, S-TALIRO and
	This paper provides a <b>formal</b> way to	destination), the initial states and the exit		translated to suitable formats for two	dReach.
	describe the scenarios, the behaviors	condition (it can be either time triggered or		falsification tools, S-TALIRO and dReach.	uncacii.
	of the vehicles and the safety	event triggered).		Taismeation tools, 5 Themo and arcaem	
	requirements. The formalization is	event triggerea).		S-TALIRO is a statistical model checking	Validation:
	used for falsification (i.e., to find	All the Behaviors of the traffic objects are		tool which gives robustness values of the	Three case studies are conducted to
	scenarios that violates the safety	modeled in one hybrid automaton.		satisfaction, denoting how good it	show that this method can detect
1	requirement).	,		satisfies (positive value) the requirement	controller faults.
	,	A logical scenario can be instantiated into a		or how bad it violates the requirement	
		concrete scenario by giving fixed values to the		(negative value). Scenarios with low	
		initial states.			

	positive robustness values can also be
The traffic laws (e.g., speed limitations) are	considered as risky scenarios.
modeled by Metric Temporal Logic (MTL).	
	dReach is based on model checking. It
	will provide either an assertion "safe" or
	a counterexample that violates the
	requirement.
	S-RALIRO runs faster than dReach,
	however, S-RALIRO cannot guarantee
	completeness.

Table 9. Other methods

#	Purpose	Scenario definition	Criticality definition& Surrogate Measure	Solution	Other key observations
[90]	Activity: Simulation + fault injection	A scenario in this paper refers to one	If a fault was injected to the AD system at	DriveFI will decide which faults to be	Required knowledge:
Driv	Phase: HARA for the preliminary	simulation run with fixed time interval.	a particular time instance in one driving	injected to one scenario at which time	1) A given concrete scenario
eFI	architecture or the verification of the	Examples of simulator include Carla and	scenario, and this fault will lead to an	instance. If the simulation shows that the	2) Functional models of the ADS
	resilience of the AD system.	DriveSim.	accident, this fault is defined as a safety	injected fault leads to an accident, the fault	3) Fault model of the ADS
	<b>SOI:</b> the whole system		critical fault and the scene at this time	and the scene are identified as safety	4) A simulator (Carla & DriveSim)
		A scene is a snapshot of one scenario at a	instance is defined as a safety critical	critical.	5) Predefined KPIs
	DriveFI is a fault injection engine to	specific time instance.	scene.		,
	fast identify safety critical faults of			The proposed method to select the injected	
	the AD systems and the	Detailed model of a scenario is not given in	To judge the criticality of a scene, it	faults:	Validation:
	corresponding critical scenes. It can	this paper.	calculates the difference between stop	A Dynamic Bayesian Network (DBN) model	In a case study, comparing to random
	be used for the safety analysis (e.g.,		distance and safe distance (the distance	is designed and trained to represent the	FI, DriveFI finds much more safety-
	HARA) phase.	Covered layers: mainly focus on the	that the ego vehicle can travel without a	relation between relevant states (internal	critical faults with much less time.
		implementation. Other layers are provided	collision) on both lateral and longitudinal	and external) and the controlled values	
	Fault injection is <b>out of the scope</b> of	by the simulator (e.g., 1, 2, 4, 5).	directions. If the stop distance is larger	(e.g., steering angle, acceleration and	Scenarios are pre-defined. DriveFI can
	this literature review.		than the safety distance, the scene will be	brake)	only find safety critical scenes from
			considered as critical.	A simulation trace will be derived by	the given scenario.
				running the ego vehicle in the given	
				concrete scenario without any injected	
				faults.	
				At each time step of this simulation trace,	
				the states will be given to the trained DBN	
				model together with an injected fault. The	
				DBN model will accordingly estimate the	
				control output of the ego vehicle for the	
				next time step.	
				The behavior of the ego vehicle at the next	
				time step is estimated via a vehicle	
				dynamic model. Based on this behavior,	
				criticality will be checked. If it is critical,	
[04]	Astista December Constitution	Comparing to most complicately the first of the selection	The made assumed after a constant	this fault and this time step will be logged.	Page de la contacta d
[91]	Activity: Reasoning & ontology	Scenario is not explicitly defined in this	The main purpose of the proposed	During validation process, experts should check all the combinations of factors within	Required knowledge:
	design (influential factors analysis)	paper. The validation space can be	approach is to find emergent effects that cause some combinations of those factors		1) Experience with a variety of
	Phase: system validation	represented with four dimensions, namely ODD, OEDR (Object and Event Detection		the four-dimensional validation space.	autonomous vehicle projects
	This article lists the factors that need		to cause unexpected and dangerous		Validation:
		and Response), Maneuvers, and Fault	results.		
	to be considered during the	Management. ODD relates to the			No validation

	validation (i.e., the validation space)	environment, OEDR and Maneuvers relate			
	of highly autonomous vehicles in a	to the intended functionality of the ego			
	systematic way, according to the	vehicle, where OEDR focuses on the			
	authors' multiple relevant project	perception and prediction; and the			
	experience.	Maneuvers dimension focuses on planning			
	•	and control.			
	This paper is considered as out of the				
	scope since it only says what aspects	ODD factors include operational terrain,			
	need to be considered to validate	Environmental and weather conditions,			
	automated vehicles, but not a	operational infrastructure, rules and			
	concrete method to identify critical	expectations, and distributions of			
	scenarios.	operational state space elements.			
		Covered layers: 1,2,3,4,5			
[80]	Activity: test suite reduction during	Covered layers: The examples cover layers	Criticality is not clearly defined in this	This paper mentions three principles to	Required knowledge:
Fun	Instantiation	1,4,5.	paper.	reduce the size of the test suite.	(1) Which parameters are (or are
c.	Phase: system V&V	The proposed test suite reduction method		(1) Testing for only one function (e.g.,	not) influential for which
Dec	<b>SOI:</b> the whole system	can be applied to any test case generation	It is not the main focus of this paper.	perception, decision making or	functions.
omp		method as long as a concrete scenario is		control) may shrink the parameter	(2) Which function may request a
	Given a logical scenario, the	modeled as a vector of relevant		space since some parameters are only	lower test coverage
	proposed method tries to reduce the	parameters.		influential on particular functions. E.g.,	
	number of generated test cases,			illumination will not affect the	
	while guaranteeing N-wise coverage.			performance of the trajectory	Validation:
				following function.	This method is verified on 9 logical
	The method decomposes the whole			(2) Less complex subsystems may require	scenarios. The results show that the
	AD/ADAS function into several sub-			a smaller test coverage.	functional decomposition approach
	functions. Each sub-function will be			(3) The test of the perception layers can	potentially reduces the size of the
	affected by only a subset of the total			be aggregated for a set of similar	required test suite by a factor of 20,,
	factors of a logical scenario. Testing			scenarios. E.g., vehicle detection	130, depending on the required test
	the sub-functions one by one may			function can be tested only once (with	coverage.
	reduce the total number of required			one aggregated test suite) for all the	-
	test cases w.r.t. coverage.			logical scenarios on a two-lane	It is not verified if the reduced test
	-			highway, since they assume that the	suite can still find the same number of
	It is <b>out of the scope</b> of the survey,			perception functions will be affected	hazards.
	since it does not talk about the			by the same set of factors within those	
	identification of critical scenarios.			scenarios.	This paper points out that the majority
	However, this topic is highly relevant.				of parameters with a high number of
	, , ,				possible values only have an influence
					on the perception functions.

**Activity:** Assessment Phase: system validation **SOI:** the whole system

> The paper is **out of the scope**. It talks about the assessment of automated driving function without the identification of critical scenarios. However, it provides an interesting perspective to evaluate automate driving function.

> a scenario-based assessment approach based on real world driving field data of both human driving and automated driving.

The method uses human driving behavior as a reference for the assessment of automated driving. Covered layer: 4 + the behavior of the ego vehicle

In the scenario classification method, a scenario has three representations: (1) time series sensor data; (2) extracted feature; and (3) classified functional scenarios (i.e., the labels, e.g., cut-in, lane change).

Suitable features are: 1. Extended features (e.g. criticality-indicators such as Time-To-Collision (TTC) or the estimated time to the next Cut-In maneuver of a traffic participant) from real world driving data; 2. Derivatives of extended features; 3. Segmentation of the extended features.

The finally used features are selected by the filter and wrapper method.

In this paper, they use field operation test data.

This paper does not explicitly talk about criticality.

The AD function under a functional scenario is assessed according to its behavior deviation from the human driving behavior.

The deviation is assessed on some predefined performance KPIs. In the vehicle following scenario longitudinal acceleration and time headway are used.

To quantify the deviation from normal driving behavior, the quantitative measure 'effect size' (calculated based on the means and variances of the performance KPIs) is proposed in the paper. An effect size less than dsmall = 0.2 can be considered as a 'small' influence.

## Assessment process:

- (1) a scenario classifier is trained by expert knowledge. The input feature is | 2) Real driving data/measurement for extracted from time series sensor data. The scenario classes are labelled by experts.
- (2) Both human driving data and automated driving data are classified into a set of predefined classes (i.e., free driving, vehicle following, lane change and cut in)
- (3) Under each class, the differences (in terms of the predefined KPIs) between human driving behavior and automated driving behavior are used as the metrics to assess the automated driving function.

## Required knowledge:

- 1) Scenarios and scenario classes
- both human driving and automated driving
- 3) Expert knowledge to label scenarios.
- 4) Expert knowledge to design the feature.
- 5) KPIs for the statistical comparison between human driving behavior and automated driving behavior under one scenario class (i.e., functional scenario)

Validation: A case study is used to evaluate the performance of the scenario classifier and the show the assessment result.

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