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Multi-position RF MEMS Tunable Capacitors using Laterally-Moving Sidewalls of 3-D Micromachined Transmission Lines

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Multi-Position RF MEMS Tunable Capacitors using Laterally-Moving Sidewalls of 3D-Micromachined Transmission Lines

Umer Shah, Student Member, IEEE, Mikael Sterner, and Joachim Oberhammer, Senior Member, IEEE

Abstract—This paper presents a novel concept of RF MEMS tunable capacitors based on the lateral displacement of the sidewalls of a three-dimensional micromachined coplanar transmission line. The tuning of a single device is achieved in multiple discrete and well-defined tuning steps by integrated multi-stage MEMS electrostatic actuators that are embedded inside the ground layer of the transmission line. Three different design concepts, including devices with up to 7 discrete tuning steps up to a tuning range of 58.6 to 144.5 fF (C_{max}/C_{min} = 2.46), have been fabricated and characterized. The highest Q-factor, measured by a weakly-coupled transmission-line resonator, was determined as 88 at 40 GHz and was achieved for a device concept where the mechanical suspension elements were completely decoupled from the RF signal path. These devices have demonstrated high self-actuation robustness with self-actuation pull-in occurring at 41.5 dBm and 47.8 dBm for mechanical spring constants of 5.8 N/m and 27.7 N/m, respectively. Nonlinearity measurements revealed that the IIP3 for all discrete device states is above the measurement-setup limit of 68.5 dBm for our 2.5-GHz IIP3 setup, with a dual-tone separation of 12 MHz. Based on capacitance/gap/spring measurements, the IIP3 was calculated for all states to be between 71 and 91 dBm. For a mechanical spring design of 5.8 N/m, the actuation and release voltages were characterized as 30.7 V and 21.15 V, respectively, and the pull-in time for the actuator bouncing to drop below 8% of the gap was measured to be 140 µs. The mechanical resonance frequencies were measured to be 5.3 kHz and 17.2 kHz for spring constant designs of 5.8 N/m and 27.7 N/m, respectively. Reliability characterization exceeded 1 billion cycles, even in an uncontrolled atmospheric environment, with no degradation in the pull-in/pull-out hysteresis behavior being observed over these cycling tests.

Index Terms—RF MEMS, switched capacitor, tunable capacitor, micromachined transmission line, micromachining.

I. INTRODUCTION

Tunable capacitors form an integral part of frequency-agile microwave systems. Micromachined RF/Microwave tunable devices, often referred to as RF micro-electromechanical systems (MEMS), are gaining considerable interest and are under active development due to their superior performance when compared to their solid state counterparts, despite recent improvements in quality factor and self-resonance frequency [1], [2], and also linearity and tuning ratio of solid-state varactor diodes [3]. MEMS tunable capacitors have shown the potential to replace solid-state varactor diodes in applications such as:

- phase shifters [4], voltage controlled oscillators, tunable filters [5] and impedance matching networks [6] because of their ability of near ideal signal handling behavior, low power consumption, low loss and large bandwidth [7]. These devices also have the ability to achieve high self resonance frequencies [8]. In the literature, four different principles have been shown to implement MEMS tunable capacitors:

1) Tunable parallel-plate capacitors, consisting of a fixed electrode and an electrode moved by an integrated MEMS actuator, which can either be utilized in analog tuning, or as a RF MEMS switched capacitors [9], [10].

2) Tunable interdigital capacitors, consisting of two comb-like electrode structures of which one can be moved by a MEMS actuator, can achieve better tuning linearity and a larger tuning range, but have a lower quality factor at high frequencies, lower self resonance frequencies and occupy a larger area [11] as compared to the parallel plate approach [8].

3) Switched capacitor banks [12], [13] in which, MEMS switches are used to select fixed metal-insulator-metal (MIM) or metal-air-metal (MAM) capacitors out of a capacitor bank.

4) A fourth concept consists of changing the dielectric loading of a transmission line by moving a dielectric block [14]. The authors have recently implemented this concept for a low-loss MEMS-movable dielectric-block phase shifter [4], [15].

From a circuit point of view, digital tuning is most often preferred over analog tuning, as it provides well defined capacitances and is robust to the actuation voltage. Whereas, analog tunable capacitors require accurate control of the actuation voltage, if not a feedback mechanism, and typically have lower linearity and a lower maximum/minimum capacitance ratio. Thus, analog tuning is typically mimicked by switched capacitor banks [12], [13].

Recently, RF MEMS-reconfigurable capacitor banks have achieved some success in commercial RF systems [16]. Sub-microsecond switching times have also been achieved by utilizing miniature capacitive beams [9], [17]. It has also been shown that using a metal-air-metal (MAM) capacitor configuration i.e. removing the isolation layer in the MEMS actuator, results in low losses [18] and reliability improvement [10], [19].

The quality factor and tuning range are important parameters for tunable capacitors, and the most remarkable achieve-
TABLE I

<table>
<thead>
<tr>
<th>Device Technology</th>
<th>Capacitance ratio</th>
<th>Quality factor (freq.)</th>
<th>Switching time</th>
</tr>
</thead>
<tbody>
<tr>
<td>MEMS [11]</td>
<td>8.4 : 1</td>
<td>35 (2 GHz)</td>
<td>6 ms</td>
</tr>
<tr>
<td>MEMS [8]</td>
<td>1.9 : 1</td>
<td>100 (34 GHz)</td>
<td>NA</td>
</tr>
<tr>
<td>MEMS [9]</td>
<td>2.3 : 1</td>
<td>50 (20 GHz)</td>
<td>400 ns</td>
</tr>
<tr>
<td>MEMS [10]</td>
<td>2 : 1</td>
<td>225 (X-Ku band)</td>
<td>8 µs</td>
</tr>
<tr>
<td>CMOS-MEMS [20]</td>
<td>4.6 : 1</td>
<td>&gt; 300 (1.5 GHz)</td>
<td>NA</td>
</tr>
<tr>
<td>MEMS [18]</td>
<td>3 : 1</td>
<td>10 (10 GHz)</td>
<td>NA</td>
</tr>
<tr>
<td>MEMS [21]</td>
<td>2.8 : 1</td>
<td>8.8 (1 GHz)</td>
<td>NA</td>
</tr>
<tr>
<td>MEMS [17]</td>
<td>3 : 1</td>
<td>90 (20 GHz)</td>
<td>200 ns</td>
</tr>
<tr>
<td>MEMS [19]</td>
<td>9 : 1</td>
<td>100 (C-X band)</td>
<td>50 µs</td>
</tr>
<tr>
<td>MEMS [22]</td>
<td>20 : 1</td>
<td>85 (3.127 GHz)</td>
<td>&lt;10 µs</td>
</tr>
<tr>
<td>CMOS-MEMS [23]</td>
<td>63 : 1</td>
<td>160 (1 GHz)</td>
<td>600 µs</td>
</tr>
<tr>
<td>CMOS [1]</td>
<td>1.6 : 1</td>
<td>&gt; 100 (24 GHz)</td>
<td>NA</td>
</tr>
<tr>
<td>GaAs [3]</td>
<td>9 : 1</td>
<td>50 (2 GHz)</td>
<td>NA</td>
</tr>
<tr>
<td>SiC [24]</td>
<td>6 : 1</td>
<td>160 (2 GHz)</td>
<td>NA</td>
</tr>
<tr>
<td>CMOS [25]</td>
<td>7.7 : 1</td>
<td>35 (1 GHz)</td>
<td>NA</td>
</tr>
<tr>
<td>MEMS (this work)</td>
<td>1.48 : 1</td>
<td>80 (40 GHz)</td>
<td>140 µs</td>
</tr>
</tbody>
</table>

This paper presents a new concept of MEMS capacitors tunable in multiple discrete and well-defined steps, implemented by in-plane moving of the ground side-walls of a 3D-micromachined coplanar waveguide transmission line. The MEMS actuators are completely embedded in the ground layer of the transmission line, and fabricated using a single-mask silicon-on-insulator (SOI) RF MEMS fabrication process, originally developed by the authors for switches [26]. The authors have shown basic ideas of tunable capacitors based on moving sidewalls at previous conferences [27], [28], including an attempt of building a filter on such a tuning technology [29].

The present paper analyzes and compares three fundamental concepts of moveable-sidewall tunable capacitors in detail, where the tuning is achieved by: Design I: bending the mechanically compliant ground sidewall; Design II: single and multistage lateral movement of the ground sidewalls with the signal routed over the mechanical springs; Design III: lateral movement of the ground sidewalls with an actuation mechanism de-coupled from the RF signal path. This paper is primarily focusing on the third concept, whose evaluation data is published here for the first time, as it achieves, by far, the best performance due to de-coupled RF and MEMS-actuation functional elements. It is shown that this novel tunable-capacitor concept achieves low insertion loss, a high quality factor, high reliability, high linearity and high self-actuation robustness, evaluated up to 40 GHz.

**II. CONCEPT AND IMPLEMENTATIONS**

The basic function of the capacitor, shown in Fig. 1, comprises the changing of the capacitive loading of a three-dimensional micromachined coplanar waveguide transmission line by a laterally moveable section of the ground layer sidewall, which is achieved by integrated MEMS actuators. This translates to a change of the capacitive part in the transmission line equivalent circuit model. The MEMS actuators are completely embedded in the ground layer of the micromachined transmission line thereby not adding any additional discontinuity in the slots, in contrast to conventional MEMS capacitors and switches that often employ biasing lines and electrodes in the signal-to-ground gap. One of the key advantages of the proposed concept is that the tuning of the capacitors is done in multiple, well-defined discrete tuning steps, which unifies the advantages of analog tuning (high resolution between minimum and maximum capacitance) and digital tuning (well-defined capacitances without feedback mechanism, actuation voltage robustness, high linearity, self-actuation robustness), even for a single device, i.e. without requiring area-consuming capacitor banks. This is achieved by stacking multiple actuators, which also offers the benefit of extended tuning range, actuating both sides alone for asymmetrical operation, creating intermediate overall capacitance steps. Such a slight asymmetry does not result in significant line imbalance, which was verified by mode-analysis, neither do the measurement indicate any unexpected behavior. The tuned RF capacitor is composed of a pure metal-air-metal (MAM) geometry that avoids dielectric charging. Also, the actuation mechanism is based on an all-metal design, i.e. the actuators do not require any dielectric layers that are prone to dielectric charging and thus decrease reliability and actuation voltage repeatability [30]. Instead, stops are used to avoid actuation-electrode short circuit. A further reliability-enhancing feature of the design is the utilization of monocrystalline silicon as the core-structural material for all moving parts, which
Table II
Overview of the Advantages and Disadvantages of the Three Design Concepts

<table>
<thead>
<tr>
<th>Advantages common to Design I, Design II and Design III</th>
<th>Design I</th>
<th>Design II</th>
<th>Design III</th>
</tr>
</thead>
<tbody>
<tr>
<td>Advantages</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Multi-step digital tuning.</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>Accurately defined and reproducible tuning states.</td>
<td></td>
<td></td>
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</tr>
<tr>
<td>3D MEMS transmission line (metal covered silicon core with decreased dielectric losses).</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>Actuator embedded in ground layer (actuation elements are invisible to wave propagation).</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>All metal design (no dielectric layer between actuator and electrode; no charging).</td>
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<td></td>
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<tr>
<td>Metallized silicon core (high reliability, temperature compensation).</td>
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<tr>
<td>No need for DC bias on the signal line.</td>
<td></td>
<td></td>
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<tr>
<td>Single mask fabrication process.</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>Additional advantages individual to Design I, Design II and Design III</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Design I</td>
<td>Design II</td>
<td>Design III</td>
<td></td>
</tr>
<tr>
<td>Advantages</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Extended tuning range by stacking actuator stages.</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Number of states independent of required transmission line length.</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Disadvantages individual to Design I, Design II and Design III</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Design I</td>
<td>Design II</td>
<td>Design III</td>
<td></td>
</tr>
<tr>
<td>Disadvantages</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Low capacitance ratio due to bending and not displacement of the capacitive element.</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Increased loss due to RF signal routing via mechanical springs.</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>Low Q-factor.</td>
<td></td>
<td></td>
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</tr>
</tbody>
</table>

is then metallized. As the metallization is symmetrical on the sidewalls, the devices are to a large extent temperature-compensated by design. In contrast to many conventional MEMS tunable capacitors, the signal line of the transmission line is not used for DC-biasing the actuation mechanism. For two of the three presented design concepts, the RF ground shares the same potential as the DC ground and the DC bias occurs on electrodes outside the RF signal path. For the third design, even the DC ground is decoupled from the RF ground. Furthermore, a benefit of 3D-micromachined transmission lines is reduced substrate losses, as the electric field lines are mainly confined to the free space above the substrate, resulting in low overall insertion loss [31]. The fabrication of these laterally-moving SOI RF MEMS devices is simple, as all transmission line and tuning elements are fabricated using a single photolithographical step.

Three different designs, exploring different ways of moving the ground layer sidewalls, have been implemented for this novel tunable capacitor concept, and are introduced in the following subsections. Furthermore, Table II lists the general advantages and disadvantages of the three different design implementations. In general, it should be noted that the capacitance values and the tuning range are higher for 3D-micromachined transmission lines with sidewall metallization, but the Q-factor is lower as compared to 3D-micromachined transmission lines with top metallization only, i.e. planar transmission lines suspended above the substrate. The self resonance frequency of the devices is dependent on the length of the device. By increasing the length of the device both the inductance and the capacitance increases thus reducing the self resonance frequency.

A. Design I: Tuning by Bending the Ground Sidewall

Fig. 2 shows a 3D sketch of this tunable capacitor concept. This design uses a 3D transmission line (signal line width, gap, height = 80 µm, 90 µm, 30.5 µm) where also the sidewalls are covered by metal, thereby forming a parallel plate capacitor to the ground with a relatively low fringing-field part (plate height: 30.5 µm; gap: 2 µm non-actuated, 4 µm in central part when actuated; length: 600 µm; thickness: 5 µm). The tuning is achieved by bending of the compliant sidewall with an electrostatic actuator, by applying a DC voltage between the actuation electrode and the ground plane. In principal, analog tuning is possible, but the presented designs were operated as switched capacitors, i.e. the capacitive element pulls in until touching the stoppers, which are in place to avoid any short circuit between the electrode and the actuator. As a tunable sidewall is arranged on each side of the signal line, the tunable capacitor has a total of three different states. For this device concept, only a low capacitance ratio can be achieved as the ground sidewall is not deflected over its whole length, and as it is more difficult to stack actuators for multiple discrete steps as compared to the other tuning concepts. The fabricated prototype device shown in Fig. 3 had an overall transmission line length of 820 µm including the probe pads.
B. Design II: Lateral Movement of Ground Sidewall with Signal Routing over Mechanical Springs

For Design II, the ground sidewall section is moved uniformly over its entire length, and the mechanical compliance is achieved by additional mechanical springs, as shown in the 3D drawing in Fig. 4. This design also utilizes 3D transmission lines (signal line width, gap, height = 80 µm, 90 µm, 30.5 µm) with metal-coverage on the sidewalls forming the capacitor (plate height: 30.5 µm; gap: 6 µm non-actuated, 2 µm when all stages are actuated; length: 600 µm; movable sidewall width: 20 µm; spring thickness: 5 µm). As the moveable sidewalls are connected to the ground plane via mechanical springs, the RF ground signal is also routed via the folded springs, which results in limited RF performance due to the increased overall series resistance of the capacitor. This design concept with uniformly moving sidewalls allows for lateral stacking of actuator stages, which results in larger sidewall movement, i.e. a extended tuning range, in accurately defined discrete steps for each actuation stage. The increased displacement can be achieved at medium actuation voltages as the total movement is split in smaller parts through sequential operation of the actuators, as shown in Fig. 5 for a two-stage design. For actuating a subsequent stage, all the previous stages have to be actuated. Thus, in contrast to a conventional switched capacitor, this concept allows multiple states. In addition to the multi-states achieved by multi-stage actuators, this concept offers additional capacitance states as the the device can be actuated asymmetrically, i.e. each side of the symmetrically duplicated design can be actuated independently. In total, a number of $2^n - 1$ states can be achieved with $n$ being the number of single-side actuation stages. It should be noted that the length of the tunable capacitor, and thus its insertion loss, is independent of the number of actuation stages, which is a unique property for a digitally controlled tunable capacitor. SEM pictures of implementations with two stage and three
Fig. 6. SEM pictures of fabricated prototype tunable capacitors of Design II: (a) implementation with two-stage actuator (5 discrete tuning states); and (b) implementation with three-stage actuator (7 discrete tuning states).

stage actuators, resulting in 5 and 7 capacitance states, respectively, are shown in Fig. 6 with an overall transmission line length of 1 mm including the probe pads.

C. Design III: Lateral Movement of Ground Sidewall with Additional Capacitive Coupling to Ground

The major disadvantage of Design II is that the RF signal is routed via the thin and long mechanical springs, increasing the overall insertion loss. In Design III, shown in Fig. 7, the mechanical springs are completely decoupled from the RF signal, i.e., the RF ground signal is coupled capacitively from the fixed ground layer to the moving ground sidewall, and the mechanical springs are connected to isolated islands behind the moving sidewalls. This results in much reduced series resistance, and thus lower insertion loss and higher Q, of the tunable capacitor as compared to the Designs II. Also, the mechanical spring length and thus stiffness and actuation voltage can be designed without implications on the RF performance. For the prototypes evaluated in this paper, the 3D transmission line of Design III is implemented with top metallization only (signal line width, gap, suspension height = 130 µm, 130 µm, 30 µm), as it was found that the transmission lines of Designs I and II had higher losses due to their relatively thin metallization layer on the sidewalls. Thus, this 3D-micromachined transmission-line implementa-

Fig. 7. Design III: 3D illustration of ground sidewall integrated tunable capacitor with ground capacitive coupling, completely de-coupling the mechanical from the RF functional elements. This design concept achieves best performance of all the presented moving-sidewall tunable-capacitor concepts, and is therefore most extensively investigated in this paper.

Fig. 8. Actuation states of a Design III tunable capacitor implemented with a single-stage actuator (only one side of the coplanar transmission line illustrated): (a) unactuated; and (b) actuated.

Fig. 8. Actuation states of a Design III tunable capacitor implemented with a single-stage actuator (only one side of the coplanar transmission line illustrated): (a) unactuated; and (b) actuated.

Fig. 8. Actuation states of a Design III tunable capacitor implemented with a single-stage actuator (only one side of the coplanar transmission line illustrated): (a) unactuated; and (b) actuated.
The fabricated prototype Design III is shown in Fig. 9.

III. FABRICATION

All structures are fabricated in a single-mask SOI (silicon on insulator) RF MEMS process developed by the authors and outlined in Fig. 10. A high resistivity > 3000 Ω-cm silicon on insulator (SOI) wafer is used with a device layer thickness of 30 µm, a buried oxide layer of 3 µm and a handle wafer thickness of 500 µm (Fig. 10(a)). First, the SOI device layer is structured by deep reactive ion plasma etching (DRIE) (Fig. 10(b)), followed by free etching of the moving structures by wet etching of the buried oxide layer using hydrofluoric acid (Fig. 10(c)). A 0.5 µm thick layer of gold is sputtered on the wafer using 50 nm of titanium tungsten as adhesion layer for the prototypes of Design I and Design II. The sidewall metallization thickness is as small as 50 nm, in particular for smaller openings including the capacitor gap. The sidewall thickness could in principle be improved by using electroplating or electroless plating. However, plating would not work for the narrow gaps and high aspect ratios employed in these designs, which results in large plating nonuniformities. For the prototypes of Design III, a 1 µm thick layer of gold on a 50 nm titanium as adhesion layer is evaporated using high-directivity e-beam evaporation, to achieve top-metallization only (Fig. 10(d)). Finally, the metal coating on the substrate and in the unwanted areas, for instance in the gap between the signal and the ground layer of the coplanar transmission line, is removed by electrochemically assisted selective etching of gold [34] in an electrically biased potassium iodide and sodium sulfite solution [35] Fig. 10(e). All the above wet steps are followed by a critical point drying step.

IV. MEASUREMENTS

Both the RF performance and the MEMS actuator performance of the tunable capacitors of all designs were characterized. The RF measurements of the fabricated capacitors were performed using an Agilent E8361A PNA Vector Network Analyzer calibrated using GGB Industries CS-5 calibration standard and 150 µm GSG coplanar probes and SOLT calibration. Table III shows the performance summary of the three designs, discussed in detail in the following subsections.

A. Characterization of Design I

Fig. 11 show the total insertion and return loss of the actuated and non actuated states for Design I, compared to the insertion loss of a transmission line of the same length without a tunable capacitor. The loss of the 3D micromachined transmission line alone is 1.17 dB at 20 GHz, attributed to the poor sidewall metal coverage of the fabricated prototypes. For the capacitors of Design I, the insertion loss is 1.61 dB in the actuated state and 2.07 dB in the unactuated state at 20 GHz, of which the transmission line alone contributes by 1.17 dB.
The capacitance is extracted from the S parameters by first de-embedding the probe pads and the transmission line using the procedure provided in [36]. The capacitance is then extracted by making the assumption of an equivalent T-network with a central capacitor corresponding to the 600 µm long distributed capacitor element. This corresponds to a transformation of a series of pi-networks (distributed capacitor) to an equivalent single T-network. The capacitance derived by this method from the measured S-parameters deviates from the stated values by less than 1.3% from 5 to 35 GHz. The extracted capacitance is 127 fF in the non actuated state and 104 fF in the actuated state resulting in a capacitance ratio of 1.22. This measured capacitance ratio is low because the capacitive element is only bending when it is actuated and not displaced over its entire length as for the Designs II and III. The actuation voltage was determined by measurements to 40 V for a spring constant of 21.2 N/m and 110 V for a spring constant of 66 N/m.

The capacitance ratio is much higher than for Design I, as the sidewalls in Design II are laterally moved over their entire length in contrast to bending for Design I, and due to the larger total travelling distance of 4 µm since the total movement is split into a number of smaller steps completed by successive actuators. Design II thus results in multiple, accurately defined and reproducible tuning states. The gap between the laterally moved ground plane sidewall and the rigid signal line is 2 and 6 µm in the two extreme positions. For actuating of a higher order stage, all previous stages already have to be pulled in. Different
unactuated, gap of the tunable capacitor is 600 µm including the probe pads. The length of the moving sidewall is 600 µm, the moving sidewall and the moving electrode of the coupling capacitor are 15 µm wide, and the length of the coupling capacitor is 200 µm. The top metallization thickness is 1 µm gold. The initial, i.e. unactuated, gap of the tunable capacitor is 4 µm, closing to 2 µm in the actuated state.

1) RF Characterization: The prototype devices have been implemented only with single-stage actuators and thus can be operated in three discrete tuning states. As described before, more stages can be designed to achieve more tuning steps, similar to Design II. Fig. 13 shows the insertion and return loss for Design III for the unactuated and all-actuated capacitor states. De-embedding technique [36] was used to de-embed the transmission line and the probe pads for extracting the capacitance values using the procedure described for Design I and Design II. The capacitance can be tuned from 40.53 fF in unactuated state to 60 fF in the double-side actuated state in three steps resulting in a capacitance ratio ($C_{\text{max}} / C_{\text{min}}$) of 1.48. This capacitance ratio is lower than reported for the Design II, as the overall capacitance is dominated by the fringing field in this top-metallization only implementation. The design has the potential for improved capacitance ratio which is largely depending on the travelling distance of the moving sidewall.

Thus tuning ratio can be increased by adding multiple stages as shown for Design II. For all three design concepts, the capacitance ratio could further be improved by moving the sidewall closer to signal line than the implemented 2 µm. The losses of the prototypes of Design III are much lower than for Designs I and II, since for Design III, the mechanical springs are completely isolated from the RF signal and they are no longer used for signal routing thereby reducing the total series resistance. Fig. 14 shows the capacitance extracted from the measured S-parameters compared to the capacitances extracted from the HFSS-simulated S-parameters. The third, intermediate, capacitance value is achieved for asymmetrical operation, i.e. when only one side is actuated. For comparison, Fig. 14 also shows the interpolation curves of the capacitances for fully analog tuning, simulated with Comsol Multiphysics, and fitted to both the measured capacitance values and the HFSS simulated capacitances. The ground coupling capacitor for a single end of a single moving sidewall was determined as 17.63 fF, derived from HFSS simulations of structures with and without the coupling capacitors. This ground coupling series capacitor reduces the overall value of the tuning capacitance from 92.4 fF to 40 fF in the unactuated and from 168 fF to 70 fF in the all-actuated state. The capacitance tuning ratio is minimally affected by the series coupling capacitors and changes from 1.82 to 1.75. The self resonance frequency for the prototype of Design III was observed to be 46 GHz.

A method based on loading a resonator with the capacitor is used for the determination of the $Q$. This is the recommended method for obtaining the $Q$ for low loss capacitors since the denominator in the standard S-parameter technique is very sensitive to $|S_{11}|^2$ [7]. Design III is expected to have high $Q$, for three reasons: firstly, because of the metal-air-metal parallel-plate capacitor configuration of the presented tunable capacitor concepts; secondly, because the mechanical springs are completely decoupled from the RF signal and thus reducing the series resistance, which is a major improvement over Design II; and thirdly, because the 3D-micromachined transmission line with thin sidewall metallization of the Designs I and II has been replaced by a suspended planar trans-
mission line. The quality factor of the capacitor was measured using a specifically designed weakly coupled transmission line resonator. The capacitor is placed in such a resonator with a nominal resonant frequency of 40 GHz and a known (measured) unloaded $Q_r$ of 14.88. The loaded $Q$ ($Q_l$) of the resonator/capacitor combination was extracted from the measured resonance behavior of the transmission line with the capacitor, using $Q_l = f_o/\Delta f$. The unloaded $Q$ ($Q_u$) of the combined structure is then determined by $Q_u = Q_l/(1-|S_{21}|)$ which is equal to the loaded $Q$ ($Q_u = Q_l$) if $S_{21} < -20$ dB. The unloaded capacitor $Q$ is then calculated by [7]

$$\frac{1}{Q_c} = \frac{1}{Q_u} - \frac{1}{Q_r}$$ (1)

Fig. 15 shows the transmission measurement results of the weakly coupled resonator ($S_{21} < -20$ dB) loaded with a capacitor in the two extreme states. For the first measurement, the capacitor gap to the transmission line is 4 µm and the extracted $Q_c$ is 88 at 40 GHz, and for the second measurement, the capacitor gap to the transmission line is 2 µm leading to an extracted $Q_c$ of 75.

2) Actuator Characterization: All displacement measurements for actuation voltage, resonance frequency, self-actuation and response time were performed using a Veeco Wyko NT9300 white-light interferometer, with the chip being placed in a slanting position underneath the lens of the profilometer. Fig. 16 shows the measured actuation and release curve for a tunable capacitor of Design III. Using COMSOL Multiphysics simulations with the measured dimensions of the fabricated geometry, a mechanical spring constant of 5.8 N/m was extracted. For the fabricated devices, the actuator moves by a total of 2.4 µm as compared to the nominal 2 µm. The measured average pull-in voltage, for 20 cycle measurements, is 30.70 V with a standard deviation of 1.08 V. For the releases voltage, the average is 21.15 V with a standard deviation of 1.71 V. Fig. 16 shows the agreement of the measured displacement of a complete cycle with COMSOL Multiphysics simulations based on the measured, fabricated geometry.

Fig. 17 shows the measured mechanical resonance responses of two fabricated devices of Design III with different spring constants. For a spring constant of 5.8 N/m the mechanical resonance frequency was measured to be 5.3 kHz, and a spring constant of 27.7 N/m results in a mechanical resonance frequency of 17.2 kHz.

Multiple response curves of a device with a spring constant of 5.8 N/m were also measured to characterize the response time of the actuator, and are plotted in Fig. 18. When the actuator is pulled in, it shows characteristic bouncing behavior as shown in Fig. 18(a). The actuator pull-in time to the first bouncing event is 60 µs, and the time for the actuator bouncing to drop below 8% of the gap is 140 µs. Similarly, Fig. 18(b) shows the release time measurements of the same actuator. The release is followed by multiple oscillation events implying that there is very low damping of the unpackaged device. However, by packaging the device in an overpressure or high viscosity gas environment, critical damping ($Q = 0.5$) can be achieved eliminating the ringing. Thus reducing the response time of the device [11]. A mechanical $Q$ of 3.9 was extracted by curve fitting from the response curves. The oscillation frequency is in good agreement with the measured mechanical resonance frequency of the device.

3) Power Handling, Linearity and Reliability Characterization: Even if the mechanical resonance frequency is several
orders of magnitude lower that the RF signal frequency, a high RF power might cause self actuation. The effective signal voltage corresponds to an equivalent DC voltage on the moving sidewalls, since the electrostatic force is proportional to the square of the signal voltage. The advantage of Design III over Designs I and II is that there is an additional capacitor for coupling to the ground which reduces the effective actuation force created by the signal voltage on the moving sidewalls. The self actuation robustness was determined by applying a 60 kHz low frequency power signal and the subsequent deflection was measured using a white light interferometer. Two devices of Design III, having spring constants of 5.8 N/m and 27.7 N/m, respectively, were measured for increasing power levels up to 50 dBm. Fig. 19 shows that for the device with \( k = 5.8 \) N/m, self actuation pull-in occurs at 41.5 dBm, and for the device with \( k = 27.7 \) N/m self actuation pull-in occurs at 47.8 dBm. The vicinity of the test RF frequency of 60 kHz to the mechanical resonance frequencies of 5.3 kHz and 17.2 kHz for the devices with 5.8 N/m and 27.7 N/m spring constants, respectively, stimulates an attenuated mechanical movement of the movable ground sidewalls, which attributes with an error to the self-actuation power measurement of less than 1% and less than 7% for the two spring designs, respectively. In principle, the stoppers of the actuator should limit the movement to the pull-in position, but it was noted that with high signal power levels of beyond 40 dBm, the moving sidewall can tilt which frequently created a non-reversible short-circuit to the signal line during the power level tests. The theoretical self actuation voltage was also calculated for comparison, using the modified DC pull-in voltage relation describing the DC-equivalent self-actuation voltage between the signal line and a single moving sidewall

\[
V_p = \sqrt{\frac{8kg_0^2}{27C_o}}
\]  

where the spring constant \( k \) is 5.8 N/m and 27.7 N/m for the two design implementations, respectively, the initial gap \( g_0 \) is 4.4 µm and the capacitor value \( C_o \) between the signal line and a single moving sidewall is 46.2 fF. \( V_p \) is then calculated to be 26.84 V (\( k = 5.8 \) N/m) and 58.65 V (\( k = 27.7 \) N/m). The necessary total voltage between the signal line and the RF ground for self actuation is then calculated by reversing the voltage division between the signal line capacitor \( C_o \) and the overall coupling capacitor \( C_c \) for a single sidewall: \( V_{RMS} = V_p(C_c+C_o)/C_c \). The calculated values are 62 V and 135.48 V for the 5.8 N/m and 27.7 N/m spring designs, respectively, which are equivalent to the self-actuation pull-in power levels 48.86 dBm and 55.65 dBm, respectively, which deviate by about 7 dB from the measured values. The linearity characteristic was determined by measuring the two-tone third-order intermodulation intercept point (IP3) with two signal sources and amplifiers at a center frequency of 2.5 GHz, separated by a 12 MHz offset. This offset frequency was chosen based on the availability of commercial notch
Fig. 21. Measured dual-tone fundamental and intermodulation levels versus input power for three states of a device of Design III ($f = 2.5$ GHz, $\Delta f = 12$ MHz).

Fig. 22. Calculated IIP3 for the three states of a device of Design III ($f = 2.5$ GHz), derived from measured capacitances, and the geometries of the fabricated device, and the simulated spring constants.

Fig. 23. Life-time characterization: Pull-in and pull-out voltages monitored over 1 billion cycles with $34$ V unipolar square waveform with a $35\%$ duty cycle and a cycle frequency of $1.6$ kHz for a device with $k = 5.8$ N/m of Design III, determined by white-light interferometry for measuring the pull-in/pull-out actuation hysteresis for each data point (see Fig. 16).

filters with such a bandwidth at a $2.5$ GHz center frequency. Such a notch filter is necessary in order not to overload the spectrum analyzer input [37]. Fig. 20 shows the two-tone IIP3 measurement setup using a notch filter ($f_0 = 2.5$ GHz, maximum passband insertion loss = $1.5$ dB, rejection center > $50$ dBc from $2.4970 - 2.5070$ MHz) for suppressing the two fundamental tones to avoid the influence of the nonlinearity of the spectrum analyzer itself. Furthermore, double isolators are used to avoid any nonlinearity of the power amplifiers having an adverse affect on the final IIP3 measurement, and to protect the amplifiers. The IIP3 measurements were carried out for all three states of a prototype device of Design III: unactuated, single-side (asymmetrically) actuated and double-side (symmetrically) actuated. Fig. 21 shows that the IIP3 measurements reach a common limit at $68.5$ dBm for all the three states of the capacitor. This value was also found for an IIP3 measurement of a transmission line alone. Thus, it can be assumed that the measured nonlinearity is limited by the transmission line measurement setup, and not the MEMS device. Fig. 22 shows the calculated IIP3 for the device in the three different states at $2.5$ GHz, derived from the measured capacitances, measured sidewall displacements and simulated spring constants of the three states of the device, using the following equation:

$$IIP3 = \frac{4k_1g_1^2k_2g_2^2}{\omega C_0^2[(k_2g_2^2) + \omega Z_0^2(k_1g_1^2)]} Z_0^2$$  \hspace{1cm} (3)$$

where $k_1$ and $k_2$ are the spring constants of left and right side actuators, $g_1$ and $g_2$ are the capacitor gaps of each side, $C_1$ and $C_2$ are the capacitances of each side, $Z_0$ is the characteristic impedance and $\omega$ is the angular frequency. This equation for a double-side capacitance has been derived from the single capacitance equations $IIP3 = 2k_1g_1^2/\phi C Z_0$, $\phi = -\omega C Z_0/2$ [7] where $\phi$ is the phase of the output signal.

The IIP3 of the three discrete states of the device have been determined as $71.4$, $74.4$ and $91.0$ dBm. The spring constants utilized for these calculated IIP3 values were determined by simulating the device geometry with dimensions measured from the fabricated prototypes, which is $5.8$ N/m and $5650$ N/m for the non-actuated and actuated (i.e. electrostatically clamped) state, respectively. These IIP3 values are, for all states, well above the measurement limit found for our measurement setup, which confirms the indifference of the IIP3 of the three states measured with our setup. The increase in IIP3 with the increasing capacitance seems to be counterintuitive as compared to conventional MEMS capacitor designs. The increase in IIP3 is caused due to the increase in the spring constant when one side or both sides are actuated, since they are electrostatically clamped upon actuation. The k values for Design III for one side is increased approximately by power of $5$ from $5.8$ N/m to $5650$ N/m when that side is actuated. The IIP3 equations derived above are valid for frequencies equal to or below the mechanical resonance frequencies and there is a further $40$ dB/decade decrease of the intermodulation levels above the mechanical resonance frequency.

Lifetime measurements were performed on a tunable capacitor of Design III with a spring constant of $5.8$ N/m (average actuation voltage of $30.7$ V) in an uncontrolled atmospheric environment. The device was cycled with an
actuation voltage of 34 V using a unipolar square waveform with a 35% duty cycle and a cycle frequency of 1.6 kHz. The pull-in and pull-out hysteresis curves were monitored after each decade of actuation cycles, to derive the pull-in and pull-out voltages over the lifetime. The actuation and release voltage values averaged from three actuation cycles at each measurement point are shown in Fig. 23. After the first 10 cycles, the actuation voltage remains constant at 30.5 V with little variation over the 1 billion cycles. The release voltage fluctuates more over the 1 billion cycles, eventually stabilizing at 19.5 V between 1 million to 400 million cycles and moving up to 21.5 V between 500 million to 1 billion cycles. The measurements were stopped after 8 days with more than 22 hours of accumulated pull-in time, when one billion cycles were reached without observing any failure, fatigue, or altered pull-in hysteresis. Neither the stoppers nor other actuator elements showed any signs of wear when inspected in the SEM after the lifetime measurements. The life-time characterization agrees very well with other silicon-core, all-metal RF MEMS devices developed by the authors [38].

V. CONCLUSION

This paper has demonstrated the concept of a novel RF MEMS tunable capacitors based on moving ground sidewalls of a 3D-micromachined coplanar transmission lines with integrated MEMS actuators. The device concept enables multiple tuning steps in discrete and well-defined positions. Embodiments of different device concepts were successfully demonstrated, achieving extraordinary high-Q, high reliability, high linearity, and high self actuation robustness at medium actuation voltages.

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REFERENCES

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